

# Package ‘OptSig’

October 12, 2022

**Type** Package

**Title** Optimal Level of Significance for Regression and Other  
Statistical Tests

**Version** 2.2

**Imports** pwr

**Date** 2022-06-29

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**Description** The optimal level of significance is calculated based on a decision-theoretic approach. The optimal level is chosen so that the expected loss from hypothesis testing is minimized. A range of statistical tests are covered, including the test for the population mean, population proportion, and a linear restriction in a multiple regression model. The details are covered in Kim and Choi (2020) <[doi:10.1111/abac.12172](https://doi.org/10.1111/abac.12172)>, and Kim (2021) <[doi:10.1080/00031305.2020.1750484](https://doi.org/10.1080/00031305.2020.1750484)>.

**License** GPL-2

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OptSig-package	<i>Optimal Level of Significance for Regression and Other Statistical Tests</i>
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## Description

The optimal level of significance is calculated based on a decision-theoretic approach. The optimal level is chosen so that the expected loss from hypothesis testing is minimized. A range of statistical tests are covered, including the test for the population mean, population proportion, and a linear restriction in a multiple regression model. The details are covered in Kim and Choi (2020) <doi:10.1111/abac.12172>, and Kim (2021) <doi:10.1080/00031305.2020.1750484>.

## Details

The DESCRIPTION file:

```

Package:      OptSig
Type:         Package
Title:        Optimal Level of Significance for Regression and Other Statistical Tests
Version:      2.2
Imports:      pwr
Date:         2022-06-29
Author:       Jae H. Kim <jaekim8080@gmail.com>
Maintainer:  Jae H. Kim <jaekim8080@gmail.com>
Description:  The optimal level of significance is calculated based on a decision-theoretic approach. The optimal level is cho
License:      GPL-2

```

Index of help topics:

```

Opt.sig.norm.test      Optimal significance level calculation for the
                        mean of a normal distribution (known variance)
Opt.sig.t.test         Optimal significance level calculation for
                        t-tests of means (one sample, two samples and
                        paired samples)
OptSig-package         Optimal Level of Significance for Regression
                        and Other Statistical Tests
OptSig.2p              Optimal significance level calculation for the

```

OptSig.2p2n	test for two proportions (same sample sizes) Optimal significance level calculation for the test for two proportions (different sample sizes)
OptSig.Boot	Optimal Significance Level for the F-test using the bootstrap
OptSig.BootWeight	Weighted Optimal Significance Level for the F-test based on the bootstrap
OptSig.Chisq	Optimal Significance Level for a Chi-square test
OptSig.F	Optimal Significance Level for an F-test
OptSig.Weight	Weighted Optimal Significance Level for the F-test based on the assumption of normality in the error term
OptSig.anova	Optimal significance level calculation for balanced one-way analysis of variance tests
OptSig.p	Optimal significance level calculation for proportion tests (one sample)
OptSig.r	Optimal significance level calculation for correlation test
OptSig.t2n	Optimal significance level calculation for two samples (different sizes) t-tests of means
Power.Chisq	Function to calculate the power of a Chi-square test
Power.F	Function to calculate the power of an F-test
R.OLS	Restricted OLS estimation and F-test
data1	Data for the U.S. production function estimation

The package accompanies the paper: Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach. Abacus. Wiley.

It provides functions for the optimal level of significance for the test for linear restriction in a regression model.

Other basic statistical tests, including those for population mean and proportion, are also covered using the functions from the pwr package.

#### Author(s)

Jae H. Kim <jaekim8080@gmail.com>

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#### References

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale, NJ: Lawrence Erlbaum.

Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

### See Also

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

### Examples

```
data(data1)
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)
# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(0.94,nrow=1)
# Model Estimation and F-test
M=R.OLS(y,x,Rmat,rvec)

# Degrees of Freedom and estimate of non-centrality parameter
K=ncol(x)+1; T=length(y)
df1=nrow(Rmat);df2=T-K; NCP=M$ncp

# Optimal level of Significance: Under Normality
OptSig.F(df1,df2,ncp=NCP,p=0.5,k=1, Figure=TRUE)
```

---

data1

*Data for the U.S. production function estimation*

---

### Description

US production, captal, labour in natrual logs for the year 2005

### Usage

```
data("data1")
```

### Format

A data frame with 51 observations on the following 3 variables.

lnoutput natrual log of output

lnlabor natrual log of labor

lncapital natrual log of capital

**Details**

The data contains 51 observations for 50 US states and Washington DC

**Source**

Gujarati, D. 2015, *Econometrics by Example*, Second edition, Palgrave.

**References**

See Section 2.2 of Gujarati (2015)

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach, *Abacus: a Journal of Accounting, Finance and Business Studies*. Wiley. <<https://doi.org/10.1111/abac.12172>>

**Examples**

```
data(data1)
```

---

Opt.sig.norm.test	<i>Optimal significance level calculation for the mean of a normal distribution (known variance)</i>
-------------------	--

---

**Description**

Computes the optimal significance level for the mean of a normal distribution (known variance)

**Usage**

```
Opt.sig.norm.test(ncp=NULL,d=NULL,n=NULL,p=0.5,k=1,alternative="two.sided",Figure=TRUE)
```

**Arguments**

ncp	Non-centrality parameter
d	Effect size, Cohen's d
n	Sample size
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, $k = L_2/L_1$ , default is $k = 1$
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of k and p

Either ncp or d value should be given.

In a general term, if  $X \sim N(\mu, \sigma^2)$ ; let  $H_0: \mu = \mu_0$ ; and  $H_1: \mu = \mu_1$ ;

$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$

$d = (\mu_1 - \mu_0)/\sigma$ : Cohen's d

**Value**

alpha.opt      Optimal level of significance  
 beta.opt        Type II error probability at the optimal level

**Note**

Also refer to the manual for the pwr package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2019). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.

Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
Opt.sig.norm.test(d=0.2,n=60,alternative="two.sided")
```

---

Opt.sig.t.test	<i>Optimal significance level calculation for t-tests of means (one sample, two samples and paired samples)</i>
----------------	---

---

**Description**

Computes the optimal significance level for the test for t-tests of means

**Usage**

```
Opt.sig.t.test(ncp=NULL,d=NULL,n=NULL,p=0.5,k=1,
              type="one.sample",alternative="two.sided",figure=TRUE)
```

**Arguments**

ncp	Non-centrality parameter
d	Effect size
n	Sample size
p	prior probability for H0, default is $p = 0.5$
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
type	Type of t test : one- two- or paired-sample
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of k and p

Either ncp or d value should be given, with the value of n.

In a general term, if  $X \sim N(\mu, \sigma^2)$ ; let  $H0: \mu = \mu_0$ ; and  $H1: \mu = \mu_1$ ;

$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$

$d = (\mu_1 - \mu_0)/\sigma$ : Cohen's d

**Value**

alpha.opt	Optimal level of significance
beta.opt	Type II error probability at the optimal level

**Note**

Also refer to the manual for the pwr package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of  $\alpha = 0.05$  as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

- Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>
- Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.
- Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
Opt.sig.t.test(d=0.2,n=60,type="one.sample",alternative="two.sided")
```

---

OptSig.2p

*Optimal significance level calculation for the test for two proportions  
(same sample sizes)*

---

**Description**

Computes the optimal significance level for the test for two proportions

**Usage**

```
OptSig.2p(ncp=NULL,h=NULL,n=NULL,p=0.5,k=1,alternative="two.sided",Figure=TRUE)
```

**Arguments**

ncp	Non-centrality parameter
h	Effect size, Cohen's h
n	Number of observations (per sample)
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, $k = L_2/L_1$ , default is k = 1
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of k and p

Either ncp or h value should be specified.

For h, refer to Cohen (1988) or Champely (2017)

In a general term, if  $X \sim N(\mu, \sigma^2)$ ; let  $H_0: \mu = \mu_0$ ; and  $H_1: \mu = \mu_1$ ;

$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$

**Value**

alpha.opt	Optimal level of significance
beta.opt	Type II error probability at the optimal level



**Note**

Also refer to the manual for the pwr package,

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.

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**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>.>

**Examples**

```
OptSig.2p(h=0.2,n=60,alternative="two.sided")
```

---

OptSig.2p2n

*Optimal significance level calculation for the test for two proportions  
(different sample sizes)*

---

**Description**

Computes the optimal significance level for the test for two proportions

**Usage**

```
OptSig.2p2n(ncp=NULL,h=NULL,n1=NULL,n2=NULL,p=0.5,k=1,alternative="two.sided",Figure=TRUE)
```

**Arguments**

ncp	Non-centrality parameter
h	Effect size, Cohen's h
n1	Number of observations (1st sample)
n2	Number of observations (2nd sample)
p	prior probability for H0, default is $p = 0.5$
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of k and p

Either ncp or h value should be specified.

For h, refer to Cohen (1988) or Champely (2017)

Assume  $X \sim N(\mu, \sigma^2)$ ; and let  $H0: \mu = \mu_0$ ; and  $H1: \mu = \mu_1$ ;

$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$

**Value**

alpha.opt	Optimal level of significance
beta.opt	Type II error probability at the optimal level

**Note**

Also refer to the manual for the pwr package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt, beta.opt). The blue horizontal line indicates the case of  $\alpha = 0.05$  as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

- Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>
- Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale, NJ: Lawrence Erlbaum.
- Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
OptSig.2p2n(h=0.30,n1=80,n2=245,alternative="greater")
```

---

OptSig.anova	<i>Optimal significance level calculation for balanced one-way analysis of variance tests</i>
--------------	---

---

**Description**

Computes the optimal significance level for the test for balanced one-way analysis of variance tests

**Usage**

```
OptSig.anova(K = NULL, n = NULL, f = NULL, p = 0.5, k = 1, Figure = TRUE)
```

**Arguments**

K	Number of groups
n	Number of observations (per group)
f	Effect size
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, k = L2/L1, default is k = 1
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of k and p

For the value of f, refer to Cohen (1988) or Champely (2017)

**Value**

alpha.opt	Optimal level of significance
beta.opt	Type II error probability at the optimal level

**Note**

Also refer to the manual for the pwr package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.

Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
OptSig.anova(f=0.28,K=4,n=20)
```

---

OptSig.Boot

*Optimal Significance Level for the F-test using the bootstrap*

---

**Description**

The function calculates the optimal level of significance for the F-test

The bootstrap can be conducted using either iid resampling or wild bootstrap.

**Usage**

```
OptSig.Boot(y,x,Rmat,rvec,p=0.5,k=1,nboot=3000,wild=FALSE,Figure=TRUE)
```

**Arguments**

y	a matrix of dependent variable, T by 1
x	a matrix of K independent variable, T by K
Rmat	a matrix for J restrictions, J by (K+1)
rvec	a vector for restrictions, J by 1
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, k = L2/L1, default is k = 1
nboot	the number of bootstrap iterations, the default is 3000
wild	if TRUE, wild bootstrap is conducted; if FALSE (default), bootstrap is based on iid residual resampling
Figure	show graph if TRUE (default). No graph otherwise

**Details**

See Kim and Choi (2020)

**Value**

alpha.opt	Optimal level of significance
crit.opt	Critical value at the optimal level
beta.opt	Type II error probability at the optimal level

**Note**

Applicable to a linear regression model

The black curve in the figure plots the density under H0; The blue curve in the figure plots the density under H1.

**Author(s)**

Jae H. Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach, Abacus, Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
data(data1)
# Define Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)

# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(0.94,nrow=1)

OptSig.Boot(y,x,Rmat,rvec,p=0.5,k=1,nboot=1000,Figure=TRUE)
```

---

OptSig.BootWeight	<i>Weighted Optimal Significance Level for the F-test based on the bootstrap</i>
-------------------	--

---

**Description**

The function calculates the weighted optimal level of significance for the F-test

The weights are obtained from the bootstrap distribution of the non-centrality parameter estimates

**Usage**

```
OptSig.BootWeight(y,x,Rmat,rvec,p=0.5,k=1,nboot=3000,wild=FALSE,Figure=TRUE)
```

**Arguments**

y	a matrix of dependent variable, T by 1
x	a matrix of K independent variable, T by K
Rmat	a matrix for J restrictions, J by (K+1)
rvec	a vector for restrictions, J by 1
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
nboot	the number of bootstrap iterations, the default is 3000
wild	if TRUE, wild bootstrap is conducted (default); if FALSE, bootstrap is based on iid resampling
Figure	show graph if TRUE . No graph if FALSE (default)

**Details**

The bootstrap can be conducted using either iid resampling or wild bootstrap.

**Value**

alpha.opt	Optimal level of significance
crit.opt	Critical value at the optimal level

**Note**

Applicable to a linear regression model

**Author(s)**

Jae H. Kim

## References

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach. Abacus, Wiley. <<https://doi.org/10.1111/abac.12172>>

## See Also

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

## Examples

```
data(data1)
# Define Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)
# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(0.94,nrow=1)

OptSig.Boot(y,x,Rmat,rvec,p=0.5,k=1,nboot=1000,Figure=TRUE)
```

---

OptSig.Chisq

*Optimal Significance Level for a Chi-square test*

---

## Description

The function calculates the optimal level of significance for a Ch-square test

## Usage

```
OptSig.Chisq(w=NULL, N=NULL, ncp=NULL, df, p = 0.5, k = 1, Figure = TRUE)
```

## Arguments

w	Effect size, Cohen's w
N	Total number of observations
ncp	a value of the non-centality paramter
df	the degrees of freedom
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, k = L2/L1, default is k = 1
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

See Kim and Choi (2020)

**Value**

alpha.opt	Optimal level of significance
crit.opt	Critical value at the optimal level
beta.opt	Type II error probability at the optimal level

**Note**

Applicable to any Chi-square test Either ncp or w (with N) should be given.

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae. H Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>.>

**Examples**

```
# Optimal level of Significance for the Breusch-Pagan test: Chi-square version
data(data1)           # call the data: Table 2.1 of Gujarati (2015)

# Extract Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)

# Restriction matrices for the slope coefficients sum to 1
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(1,nrow=1)

# Model Estimation
```



```

M=R.OLS(y,x,Rmat,rvec); print(M$coef)

# Breusch-Pagan test for heteroskedasticity
e = M$resid[,1]          # residuals from unrestricted model estimation

# Restriction matrices for the slope coefficients being 0
Rmat=matrix(c(0,0,1,0,0,1),nrow=2); rvec=matrix(0,nrow=2)

# Model Estimation for the auxilliary regression
M1=R.OLS(e^2,x,Rmat,rvec);

# Degrees of Freedom and estimate of non-centrality parameter
df1=nrow(Rmat); NCP=M1$ncp

# LM stat and p-value
LM=nrow(data1)*M1$Rsq[1,1]
pval=pchisq(LM,df=df1,lower.tail = FALSE)

OptSig.Chisq(df=df1,ncp=NCP,p=0.5,k=1, Figure=TRUE)

```

---

OptSig.F

*Optimal Significance Level for an F-test*


---

## Description

The function calculates the optimal level of significance for an F-test

## Usage

```
OptSig.F(df1, df2, ncp, p = 0.5, k = 1, Figure = TRUE)
```

## Arguments

df1	the first degrees of freedom for the F-distribution
df2	the second degrees of freedom for the F-distribution
ncp	a value of of the non-centality paramter
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
Figure	show graph if TRUE (default); No graph if FALSE

## Details

See Kim and Choi (2020)

## Value

alpha.opt	Optimal level of significance
crit.opt	Critical value at the optimal level
beta.opt	Type II error probability at the optimal level

**Note**

Applicable to any F-test, following F-distribution

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae. H Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
data(data1)
# Define Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)
# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(0.94,nrow=1)
# Model Estimation and F-test
M=R.OLS(y,x,Rmat,rvec)

# Degrees of Freedom and estimate of non-centrality parameter
K=ncol(x)+1; T=length(y)
df1=nrow(Rmat);df2=T-K; NCP=M$ncp

# Optimal level of Significance: Under Normality
OptSig.F(df1,df2,ncp=NCP,p=0.5,k=1, Figure=TRUE)
```

---

OptSig.p	<i>Optimal significance level calculation for proportion tests (one sample)</i>
----------	---

---

**Description**

Computes the optimal significance level for proportion tests (one sample)

**Usage**

```
OptSig.p(ncp=NULL,h=NULL,n=NULL,p=0.5,k=1,alternative="two.sided",Figure=TRUE)
```

**Arguments**

ncp	Non-centrality parameter
h	Effect size, Cohen's h
n	Number of observations (per sample)
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of k and p

Either ncp or h value should be given

For h, refer to Cohen (1988) or Chappmely (2017)

In a general term, if  $X \sim N(\mu, \sigma^2)$ ; let  $H0:\mu = \mu_0$ ; and  $H1:\mu = \mu_1$ ;

$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$

**Value**

alpha.opt	Optimal level of significance
beta.opt	Type II error probability at the optimal level

**Note**

Also refer to the manual for the pwr package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.

Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>.>

**Examples**

```
OptSig.p(h=0.2,n=60,alternative="two.sided")
```

---

OptSig.r

*Optimal significance level calculation for correlation test*

---

**Description**

Computes the optimal significance level for the correlation test

**Usage**

```
OptSig.r(r=NULL,n=NULL,p=0.5,k=1,alternative="two.sided",Figure=TRUE)
```

**Arguments**

r	Linear correlation coefficient
n	sample size
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II error, $k = L_2/L_1$ , default is $k = 1$
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

Refer to Kim and Choi (2020) for the details of  $k$  and  $p$

In a general term, if  $X \sim N(\mu, \sigma^2)$ ; let  $H_0: \mu = \mu_0$ ; and  $H_1: \mu = \mu_1$ ;

$$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$$

**Value**

<code>alpha.opt</code>	Optimal level of significance
<code>beta.opt</code>	Type II error probability at the optimal level

**Note**

Also refer to the manual for the `pwr` package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: `(alpha.opt, beta.opt)`. The blue horizontal line indicates the case of  $\alpha = 0.05$  as a reference point.

**Author(s)**

Jae H. Kim (using a function from the `pwr` package)

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: *Abacus: a Journal of Accounting, Finance and Business Studies*. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). *Statistical power analysis for the behavioral sciences* (2nd ed.). Hillsdale, NJ: Lawrence Erlbaum.

Stephane Champely (2017). `pwr: Basic Functions for Power Analysis`. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package `OptSig`, *The American Statistician*. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
OptSig.r(r=0.2, n=60, alternative="two.sided")
```

---

OptSig.t2n	<i>Optimal significance level calculation for two samples (different sizes) t-tests of means</i>
------------	--

---

### Description

Computes the optimal significance level for two samples (different sizes) t-tests of means

### Usage

```
OptSig.t2n(ncp=NULL,d=NULL,n1=NULL,n2=NULL,p=0.5,k=1,alternative="two.sided",Figure=TRUE)
```

### Arguments

ncp	Non-centrality parameter
d	Effect size
n1	umber of observations in the first sample
n2	umber of observations in the second sample
p	prior probability for H0, default is p = 0.5
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
alternative	a character string specifying the alternative hypothesis, must be one of "two.sided" (default), "greater" or "less"
Figure	show graph if TRUE (default); No graph if FALSE

### Details

Refer to Kim and Choi (2020) for the details of k and p

Either ncp or d value should be specified.

In a general term, if  $X \sim N(\mu, \sigma^2)$ ; let  $H0: \mu = \mu_0$ ; and  $H1: \mu = \mu_1$ ;

$ncp = \sqrt{n}(\mu_1 - \mu_0)/\sigma$

$d = (\mu_1 - \mu_0)/\sigma$ : Cohen's d

### Value

alpha.opt	Optimal level of significance
beta.opt	Type II error probability at the optimal level

### Note

Also refer to the manual for the pwr package

The black curve in the figure is the line of enlightened judgement: see Kim and Choi (2020). The red dot indicates the optimal significance level that minimizes the expected loss: (alpha.opt,beta.opt). The blue horizontal line indicates the case of alpha = 0.05 as a reference point.

**Author(s)**

Jae H. Kim (using a function from the pwr package)

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach: Abacus: a Journal of Accounting, Finance and Business Studies. Wiley. <<https://doi.org/10.1111/abac.12172>>

Cohen, J. (1988). Statistical power analysis for the behavioral sciences (2nd ed.). Hillsdale,NJ: Lawrence Erlbaum.

Stephane Champely (2017). pwr: Basic Functions for Power Analysis. R package version 1.2-1. <https://CRAN.R-project.org/package=pwr>

**See Also**

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>.>

**Examples**

```
OptSig.t2n(d=0.6,n1=90,n2=60,alternative="greater")
```

---

OptSig.Weight

*Weighted Optimal Significance Level for the F-test based on the assumption of normality in the error term*

---

**Description**

The function calculates the weighted optimal level of significance for the F-test

The weights are obtained from a folded-normal distribution with mean  $m$  and standard deviation  $\delta$

**Usage**

```
OptSig.Weight(df1, df2, m, delta = 2, p = 0.5, k = 1, Figure = TRUE)
```

**Arguments**

df1	the first degrees of freedom for the F-distribution
df2	the second degrees of freedom for the F-distribution
m	a value of of the non-centality paramter, the mean of the folded-normal distribution
delta	standard deviation of the folded-normal distribution
p	prior probability for H0, default is $p = 0.5$
k	relative loss from Type I and II errors, $k = L2/L1$ , default is $k = 1$
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

See Kim and Choi (2020)

**Value**

alpha.opt	Optimal level of significance
crit.opt	Critical value at the optimal level

**Note**

The figure shows the folded-normal distribution

**Author(s)**

Jae H. Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach, Abacus, Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
data(data1)
# Define Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)
# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(0.94,nrow=1)
# Model Estimation and F-test
M=R.OLS(y,x,Rmat,rvec)

# Degrees of Freedom and estimate of non-centrality parameter
K=ncol(x)+1; T=length(y)
df1=nrow(Rmat);df2=T-K; NCP=M$ncp

OptSig.Weight(df1,df2,m=NCP,delta=3,p=0.5,k=1,Figure=TRUE)
```



---

Power.Chisq	<i>Function to calculate the power of a Chi-square test</i>
-------------	---

---

**Description**

This function calculates the power of a Chi-square test, given the value of non-centrality parameter

**Usage**

```
Power.Chisq(df, ncp, alpha, Figure = TRUE)
```

**Arguments**

df	degree of freedom
ncp	a value of of the non-centality paramter
alpha	the level of significance
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

See Kim and Choi (2020)

**Value**

Power	Power of the test
Crit.val	Critical value at alpha level of signifcance

**Note**

See Application Section and Appendix of Kim and Choi (2017)

**Author(s)**

Jae H. Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach, Abacus, Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
Power.Chisq(df=5,ncp=5,alpha=0.05,Figure=TRUE)
```

---

 Power.F

---

*Function to calculate the power of an F-test*


---

**Description**

This function calculates the power of an F-test, given the value of non-centrality parameter

**Usage**

```
Power.F(df1, df2, ncp, alpha, Figure = TRUE)
```

**Arguments**

df1	the first degrees of freedom for the F-distribution
df2	the second degrees of freedom for the F-distribution
ncp	a value of of the non-centality paramter
alpha	the level of significance
Figure	show graph if TRUE (default); No graph if FALSE

**Details**

See Kim and Choi (2020)

**Value**

Power	Power of the test
Crit.val	Critical value at alpha level of signifcance

**Note**

See Application Section and Appendix of Kim and Choi (2020)

**Author(s)**

Jae H. Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach, Abacus, Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:http://dx.doi.org/10.1016/j.jempfin.2015.08.006>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <https://doi.org/10.1080/00031305.2020.1750484.>

**Examples**

```
data(data1)
# Define Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)
# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(0.94,nrow=1)
# Model Estimation and F-test
M=R.OLS(y,x,Rmat,rvec)
# Degrees of Freedom and estimate of non-centrality parameter
K=ncol(x)+1; T=length(y)
df1=nrow(Rmat);df2=T-K; NCP=M$ncp

Power.F(df1,df2,ncp=NCP,alpha=0.20747,Figure=TRUE)
```

---

R.OLS

*Restricted OLS estimation and F-test*


---

**Description**

Function to calculate the Restricted (under H0) OLS Estimators and F-test statistic

**Usage**

```
R.OLS(y, x, Rmat, rvec)
```

**Arguments**

y	a matrix of dependent variable, T by 1
x	a matrix of K independent variable, T by K
Rmat	a matrix for J restrictions, J by (K+1)
rvec	a vector for restrictions, J by 1

**Details**

Rmat and rvec are the matrices for the linear restrictions, which a user should supply.

Refer to an econometrics textbook for details.

**Value**

coef	matrix of estimated coefficients, (K+1) by 2, under H1 and H0
RSq	R-square values under H1 and H0, 2 by 1
resid	residual vector under H1 and H0, T by 2
F.stat	F-statistic and p-value
ncp	non-centrality parameter, estimated by replacing unknowns using OLS estimates

**Note**

The function automatically adds an intercept, so the user need not include a vector of ones in x matrix.

**Author(s)**

Jae H. Kim

**References**

Kim and Choi, 2020, Choosing the Level of Significance: A Decision-theoretic Approach, Abacus, Wiley. <<https://doi.org/10.1111/abac.12172>>

**See Also**

Leamer, E. 1978, Specification Searches: Ad Hoc Inference with Nonexperimental Data, Wiley, New York.

Kim, JH and Ji, P. 2015, Significance Testing in Empirical Finance: A Critical Review and Assessment, Journal of Empirical Finance 34, 1-14. <DOI:<http://dx.doi.org/10.1016/j.jempfin.2015.08.006>>

Kim, Jae H., 2020, Decision-theoretic hypothesis testing: A primer with R package OptSig, The American Statistician. <<https://doi.org/10.1080/00031305.2020.1750484>>

**Examples**

```
data(data1)
# Define Y and X
y=data1$lnoutput; x=cbind(data1$lncapital,data1$lnlabor)
# Restriction matrices to test for constant returns to scale
Rmat=matrix(c(0,1,1),nrow=1); rvec=matrix(1,nrow=1)
# Model Estimation and F-test
M=R.OLS(y,x,Rmat,rvec)
```

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