# Package 'grpreg'

September 3, 2024

Title Regularization Paths for Regression Models with Grouped

Covariates

```
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Description Efficient algorithms for fitting the regularization path of linear
      regression, GLM, and Cox regression models with grouped penalties. This
      includes group selection methods such as group lasso, group MCP, and
      group SCAD as well as bi-level selection methods such as the group
      exponential lasso, the composite MCP, and the group bridge. For more
      information, see Breheny and Huang (2009) <doi:10.4310/sii.2009.v2.n3.a10>,
      Huang, Breheny, and Ma (2012) <doi:10.1214/12-sts392>, Breheny and Huang
      (2015) <doi:10.1007/s11222-013-9424-2>, and Breheny (2015)
      <doi:10.1111/biom.12300>, or visit the package homepage
      <a href="https://pbreheny.github.io/grpreg/">https://pbreheny.github.io/grpreg/>.</a>
BugReports https://github.com/pbreheny/grpreg/issues
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```

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## Description

Calculates the cross-validated AUC (concordance) from a "cv.grpsurv" object.

## Usage

```
## $3 method for class 'cv.grpsurv'
AUC(obj, ...)
```

## Arguments

obj A cv.grpsurv object. You must run cv.grpsurv() with the option returnY=TRUE in order for AUC to work.

For S3 method compatibility.

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#### **Details**

The area under the curve (AUC), or equivalently, the concordance statistic (C), is calculated according to the procedure described in van Houwelingen and Putter (2011). The function calls survival::concordancefit(), except cross-validated linear predictors are used to guard against overfitting. Thus, the values returned by AUC.cv.grpsurv() will be lower than those you would obtain with concordancefit() if you fit the full (unpenalized) model.

#### References

van Houwelingen H, Putter H (2011). Dynamic Prediction in Clinical Survival Analysis. CRC Press.

#### See Also

```
cv.grpsurv(), survival::survConcordance()
```

#### **Examples**

Birthwt

Risk Factors Associated with Low Infant Birth Weight

## **Description**

The Birthwt data contains 189 observations, 16 predictors, and an outcome, birthweight, available both as a continuous measure and a binary indicator for low birth weight. The data were collected at Baystate Medical Center, Springfield, Mass during 1986. This data frame is a reparameterization of the birthwt data frame from the **MASS** package.

#### **Usage**

Birthwt

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#### **Format**

The Birthwt object is a list containing four elements (X, bwt, low, and group):

bwt Birth weight in kilograms

low Indicator of birth weight less than 2.5kg

group Vector describing how the columns of X are grouped

**X** A matrix with 189 observations (rows) and 16 predictor variables (columns).

The matrix X contains the following columns:

age1,age2,age3 Orthogonal polynomials of first, second, and third degree representing mother's age in years

lwt1,lwt2,lwt3 Orthogonal polynomials of first, second, and third degree representing mother's weight in pounds at last menstrual period

white,black Indicator functions for mother's race; "other" is reference group

smoke Smoking status during pregnancy

**ptl1,ptl2m** Indicator functions for one or for two or more previous premature labors, respectively. No previous premature labors is the reference category.

ht History of hypertension

ui Presence of uterine irritability

**ftv1,ftv2,ftv3m** Indicator functions for one, for two, or for three or more physician visits during the first trimester, respectively. No visits is the reference category.

#### Source

```
https://cran.r-project.org/package=MASS
```

#### References

- Venables, W. N. and Ripley, B. D. (2002). *Modern Applied Statistics with S.* Fourth edition. Springer.
- Hosmer, D.W. and Lemeshow, S. (1989) Applied Logistic Regression. New York: Wiley

#### See Also

```
MASS::birthwt, grpreg()
```

```
data(Birthwt)
hist(Birthwt$bwt, xlab="Child's birth weight", main="")
table(Birthwt$low)
## See examples in ?birthwt (MASS package)
## for more about the data set
## See examples in ?grpreg for use of this data set
## with group penalized regression models
```

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birthwt.grpreg

Risk Factors Associated with Low Infant Birth Weight

### **Description**

This version of the data set has been deprecated and will not be supported in future versions. Please use Birthwt instead.

## Usage

birthwt.grpreg

#### **Format**

This data frame contains the following columns:

- low Indicator of birth weight less than 2.5kg
- bwt Birth weight in kilograms
- age1, age2, age3 Orthogonal polynomials of first, second, and third degree representing mother's age in years
- lwt1, lwt2, lwt3 Orthogonal polynomials of first, second, and third degree representing mother's weight in pounds at last menstrual period
- white, black Indicator functions for mother's race; "other" is reference group
- smoke smoking status during pregnancy
- ptl1,ptl2m Indicator functions for one or for two or more previous premature labors, respectively. No previous premature labors is the reference category.
- ht History of hypertension
- ui Presence of uterine irritability
- ftv1, ftv2, ftv3m Indicator functions for one, for two, or for three or more physician visits during the first trimester, respectively. No visits is the reference category.

#### See Also

Birthwt

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cv.grpreg

Cross-validation for grpreg/grpsurv

## **Description**

Performs k-fold cross validation for penalized regression models with grouped covariates over a grid of values for the regularization parameter lambda.

## Usage

```
cv.grpreg(
  Χ,
  у,
  group = 1:ncol(X),
  nfolds = 10,
  seed,
  fold,
  returnY = FALSE,
  trace = FALSE
)
cv.grpsurv(
  Χ,
  у,
  group = 1:ncol(X),
  nfolds = 10,
  seed,
  fold,
  se = c("quick", "bootstrap"),
  returnY = FALSE,
  trace = FALSE
)
```

## Arguments

Χ	The design matrix, as in grpreg()/grpsurv().
У	The response vector (or matrix), as in grpreg()/grpsurv().
group	The grouping vector, as in grpreg()/grpsurv().
	Additional arguments to grpreg()/grpsurv().
nfolds	The number of cross-validation folds. Default is 10.
seed	You may set the seed of the random number generator in order to obtain reproducible results.
fold	Which fold each observation belongs to. By default the observations are randomly assigned.

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returnY Should cv.grpreg()/cv.grpsurv() return the fitted values from the cross-validation folds? Default is FALSE; if TRUE, this will return a matrix in which the element for row is column it is the fitted value for observation if from the fold in which

for row i, column j is the fitted value for observation i from the fold in which observation i was excluded from the fit, at the jth value of lambda. NOTE: For cv.grpsurv(), the rows of Y are ordered by time on study, and therefore will not correspond to the original order of observations pased to cv.grpsurv.

trace If set to TRUE, cv.grpreg will inform the user of its progress by announcing the

beginning of each CV fold. Default is FALSE.

se For cv. grpsurv(), the method by which the cross-valiation standard error (CVSE)

is calculated. The 'quick' approach is based on a rough approximation, but can be calculated more or less instantly. The 'bootstrap' approach is more accurate,

but requires additional computing time.

#### **Details**

The function calls <code>grpreg()</code> or <code>grpsurv()</code> nfolds times, each time leaving out 1/nfolds of the data. The cross-validation error is based on the deviance; see here for more details.

For Gaussian and Poisson responses, the folds are chosen according to simple random sampling. For binomial responses, the numbers for each outcome class are balanced across the folds; i.e., the number of outcomes in which y is equal to 1 is the same for each fold, or possibly off by 1 if the numbers do not divide evenly. This approach is used for Cox regression as well to balance the amount of censoring cross each fold.

For Cox models, cv.grpsurv uses the approach of calculating the full Cox partial likelihood using the cross-validated set of linear predictors. Other approaches to cross-validation for the Cox regression model have been proposed in the literature; the strengths and weaknesses of the various methods for penalized regression in the Cox model are the subject of current research. A simple approximation to the standard error is provided, although an option to bootstrap the standard error (se='bootstrap') is also available.

As in grpreg(), seemingly unrelated regressions/multitask learning can be carried out by setting y to be a matrix, in which case groups are set up automatically (see grpreg() for details), and cross-validation is carried out with respect to rows of y. As mentioned in the details there, it is recommended to standardize the responses prior to fitting.

#### Value

An object with S3 class "cv.grpreg" containing:

cve The error for each value of lambda, averaged across the cross-validation folds.

cvse The estimated standard error associated with each value of for cve.

lambda The sequence of regularization parameter values along which the cross-validation

error was calculated.

fit The fitted grpreg object for the whole data.

fold The fold assignments for cross-validation for each observation; note that for

cv.grpsurv, these are in terms of the ordered observations, not the original

observations.

min The index of lambda corresponding to lambda.min.

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lambda.min The value of lambda with the minimum cross-validation error.

null.dev The deviance for the intercept-only model.

pe If family="binomial", the cross-validation prediction error for each value of

lambda.

#### Author(s)

Patrick Breheny

#### See Also

```
grpreg(), plot.cv.grpreg(), summary.cv.grpreg(), predict.cv.grpreg()
```

## **Examples**

```
data(Birthwt)
X <- Birthwt$X
y <- Birthwt$bwt
group <- Birthwt$group

cvfit <- cv.grpreg(X, y, group)
plot(cvfit)
summary(cvfit)
coef(cvfit) ## Beta at minimum CVE

cvfit <- cv.grpreg(X, y, group, penalty="gel")
plot(cvfit)
summary(cvfit)</pre>
```

expand\_spline

Expand feature matrix using basis splines

## **Description**

Performs a basis expansion for many features at once, returning output that is compatible for use with the grpreg() function. Returns an expanded matrix along with a vector that describes its grouping.

#### Usage

```
expand_spline(x, df = 3, degree = 3, type = c("ns", "bs"))
```

## **Arguments**

X	Features to be expanded (numeric matrix).
df	Degrees of freedom (numeric; default = 3).
degree	Degree of the piecewise polynomial (integer; default = 3 (cubic splines)).

type Type of spline, either B-spline ("bs") or natural cubic spline ("ns"; default).

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#### **Details**

expand\_spline() uses the function splines::bs() or splines::ns() to generate a basis matrix for each column of x. These matrices represent the spline basis for piecewise polynomials with specified degree evaluated separately for each original column of x. These matrices are then column-bound to form a single grouped matrix of derived features. A vector that describes the grouping present in the resulting matrix is also generated. The resulting object can be passed to grpreg().

This methodology was originally proposed by Ravikumar et al. (2009), who named it SPAM (SParse Additive Modeling).

#### Value

An object of class expandedMatrix consisting of:

- X: A matrix of dimension nrow(x) by df\*ncol(x)
- group: A vector of length df\*ncol(x) that describes the grouping structure
- Additional metadata on the splines, such as knot locations, required in order to evaluate spline at new feature values (e.g., for prediction)

#### References

• Ravikumar P, Lafferty J, Liu H and Wasserman L (2009). Sparse additive models. *Journal of the Royal Statistical Society Series B*, **71**: 1009-1030.

#### See Also

```
plot_spline() to visualize the resulting nonlinear fits
```

#### **Examples**

```
Data <- gen_nonlinear_data(n=1000)
X <- expand_spline(Data$X)
fit <- grpreg(X, Data$y)
plot_spline(fit, "V02", lambda = 0.03)</pre>
```

gBridge

Fit a group bridge regression path

#### **Description**

Fit regularization paths for linear and logistic group bridge-penalized regression models over a grid of values for the regularization parameter lambda.

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## Usage

```
gBridge(
  Χ,
  у,
  group = 1:ncol(X),
  family = c("gaussian", "binomial", "poisson"),
  nlambda = 100,
  lambda,
  lambda.min = {
     if (nrow(X) > ncol(X))
         0.001
     else 0.05
 },
  lambda.max,
  alpha = 1,
  eps = 0.001,
  delta = 1e-07,
  max.iter = 10000,
  gamma = 0.5,
  group.multiplier,
  warn = TRUE,
  returnX = FALSE,
)
```

## Arguments

Χ	The design matrix, as in grpreg.
У	The response vector (or matrix), as in grpreg.
group	The grouping vector, as in grpreg.
family	Either "gaussian" or "binomial", depending on the response.
nlambda	The number of lambda values, as in grpreg.
lambda	A user supplied sequence of lambda values, as in grpreg()'.
lambda.min	The smallest value for lambda, as in grpreg.
lambda.max	The maximum value for lambda. Unlike the penalties in grpreg, it is not possible to solve for lambda.max directly with group bridge models. Thus, it must be specified by the user. If it is not specified, gBridge will attempt to guess lambda.max, but this is not particularly accurate.
alpha	Tuning parameter for the balance between the group penalty and the $L2$ penalty, as in grpreg.
eps	Convergence threshhold, as in grpreg.
delta	The group bridge penalty is not differentiable at zero, and requires a small number delta to bound it away from zero. There is typically no need to change this value.
max.iter	Maximum number of iterations, as in grpreg.

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Tuning parameter of the group bridge penalty (the exponent to which the L1 norm of the coefficients in the group are raised). Default is 0.5, the square root. group.multiplier

The multiplicative factor by which each group's penalty is to be multiplied, as in grpreg.

warn

Should the function give a warning if it fails to converge? As in grpreg.

Return the standardized design matrix (and associated group structure informa-

tion)? Default is FALSE.

... Not used.

#### **Details**

This method fits the group bridge method of Huang et al. (2009). Unlike the penalties in grpreg, the group bridge is not differentiable at zero; because of this, a number of changes must be made to the algorithm, which is why it has its own function. Most notably, the method is unable to start at lambda.max; it must start at lambda.min and proceed in the opposite direction.

In other respects, the usage and behavior of the function is similar to the rest of the grpreg package.

#### Value

An object with S3 class "grpreg", as in grpreg.

#### References

- Huang J, Ma S, Xie H, and Zhang C. (2009) A group bridge approach for variable selection. *Biometrika*, **96**: 339-355. doi:10.1093/biomet/asp020
- Breheny P and Huang J. (2009) Penalized methods for bi-level variable selection. *Statistics and its interface*, **2**: 369-380. doi:10.4310/sii.2009.v2.n3.a10

#### See Also

```
grpreg()
```

```
data(Birthwt)
X <- Birthwt$X
group <- Birthwt$group

## Linear regression
y <- Birthwt$bwt
fit <- gBridge(X, y, group, lambda.max=0.08)
plot(fit)
select(fit)$beta

## Logistic regression
y <- Birthwt$low
fit <- gBridge(X, y, group, family="binomial", lambda.max=0.17)
plot(fit)
select(fit)$beta</pre>
```

gen\_nonlinear\_data

Generate nonlinear example data

## **Description**

Mainly intended to demonstrate the use of basis expansion models for sparse additive modeling; intended for use with expand\_spline().

## Usage

```
gen_nonlinear_data(n = 100, p = 16, seed)
```

## **Arguments**

```
n Sample size (numeric; default = 100).

p Number of features (numeric; default = 16).

seed Set to get different random data sets, passed to set.seed()
```

## **Examples**

```
Data <- gen_nonlinear_data()</pre>
```

grpreg

Fit a group penalized regression path

#### **Description**

Fit regularization paths for models with grouped penalties over a grid of values for the regularization parameter lambda. Fits linear and logistic regression models.

## Usage

```
log.lambda = TRUE,
alpha = 1,
eps = 1e-04,
max.iter = 10000,
dfmax = p,
gmax = length(unique(group)),
gamma = ifelse(penalty == "grSCAD", 4, 3),
tau = 1/3,
group.multiplier,
warn = TRUE,
returnX = FALSE,
...
)
```

### **Arguments**

alpha

X The design matrix, without an intercept. grpreg standardizes the data and includes an intercept by default.

y The response vector, or a matrix in the case of multitask learning (see details).

group A vector describing the grouping of the coefficients. For greatest efficiency and

A vector describing the grouping of the coefficients. For greatest efficiency and least ambiguity (see details), it is best if group is a factor or vector of consecutive integers, although unordered groups and character vectors are also allowed. If there are coefficients to be included in the model without being penalized, assign

them to group 0 (or "0").

penalty The penalty to be applied to the model. For group selection, one of grLasso,

grMCP, or grSCAD. For bi-level selection, one of gel or cMCP. See below for

details.

family Either "gaussian" or "binomial", depending on the response.

nlambda The number of lambda values. Default is 100.

lambda A user supplied sequence of lambda values. Typically, this is left unspecified,

and the function automatically computes a grid of lambda values that ranges

uniformly on the log scale over the relevant range of lambda values.

lambda.min The smallest value for lambda, as a fraction of lambda.max. Default is .0001

if the number of observations is larger than the number of covariates and .05

otherwise.

log.lambda Whether compute the grid values of lambda on log scale (default) or linear scale.

grpreg allows for both a group penalty and an L2 (ridge) penalty; alpha con-

trols the proportional weight of the regularization parameters of these two penalties. The group penalties' regularization parameter is lambda\*alpha, while the regularization parameter of the ridge penalty is lambda\*(1-alpha). Default is

1: no ridge penalty.

eps Convergence threshhold. The algorithm iterates until the RMSD for the change

in linear predictors for each coefficient is less than eps. Default is 1e-4. See

details.

max.iter Maximum number of iterations (total across entire path). Default is 10000. See

details.

dfmax Limit on the number of parameters allowed to be nonzero. If this limit is ex-

ceeded, the algorithm will exit early from the regularization path.

gmax Limit on the number of groups allowed to have nonzero elements. If this limit

is exceeded, the algorithm will exit early from the regularization path.

gamma Tuning parameter of the group or composite MCP/SCAD penalty (see details).

Default is 3 for MCP and 4 for SCAD.

tau Tuning parameter for the group exponential lasso; defaults to 1/3.

group.multiplier

A vector of values representing multiplicative factors by which each group's penalty is to be multiplied. Often, this is a function (such as the square root) of the number of predictors in each group. The default is to use the square root of group size for the group selection methods, and a vector of 1's (i.e., no

adjustment for group size) for bi-level selection.

warn Should the function give a warning if it fails to converge? Default is TRUE. See

details.

returnX Return the standardized design matrix (and associated group structure informa-

tion)? Default is FALSE.

... Arguments passed to other functions (such as gBridge).

#### **Details**

There are two general classes of methods involving grouped penalties: those that carry out bi-level selection and those that carry out group selection. Bi-level means carrying out variable selection at the group level as well as the level of individual covariates (i.e., selecting important groups as well as important members of those groups). Group selection selects important groups, and not members within the group – i.e., within a group, coefficients will either all be zero or all nonzero. The grLasso, grMCP, and grSCAD penalties carry out group selection, while the gel and cMCP penalties carry out bi-level selection. For bi-level selection, see also the gBridge() function. For historical reasons and backwards compatibility, some of these penalties have aliases; e.g., gLasso will do the same thing as grLasso, but users are encouraged to use grLasso.

Please note the distinction between grMCP and cMCP. The former involves an MCP penalty being applied to an L2-norm of each group. The latter involves a hierarchical penalty which places an outer MCP penalty on a sum of inner MCP penalties for each group, as proposed in Breheny & Huang, 2009. Either penalty may be referred to as the "group MCP", depending on the publication. To resolve this confusion, Huang et al. (2012) proposed the name "composite MCP" for the cMCP penalty.

For more information about the penalties and their properties, please consult the references below, many of which contain discussion, case studies, and simulation studies comparing the methods. If you use grpreg for an analysis, please cite the appropriate reference.

In keeping with the notation from the original MCP paper, the tuning parameter of the MCP penalty is denoted 'gamma'. Note, however, that in Breheny and Huang (2009), gamma is denoted 'a'.

The objective function for grpreg optimization is defined to be

$$Q(\beta|X,y) = \frac{1}{n}L(\beta|X,y) + P_{\lambda}(\beta)$$

where the loss function L is the negative log-likelihood (half the deviance) for the specified outcome distribution (gaussian/binomial/poisson). For more details, refer to the following:

- · Models and loss functions
- Penalties

For the bi-level selection methods, a locally approximated coordinate descent algorithm is employed. For the group selection methods, group descent algorithms are employed.

The algorithms employed by grpreg are stable and generally converge quite rapidly to values close to the solution. However, especially when p is large compared with n, grpreg may fail to converge at low values of lambda, where models are nonidentifiable or nearly singular. Often, this is not the region of the coefficient path that is most interesting. The default behavior warning the user when convergence criteria are not met may be distracting in these cases, and can be modified with warn (convergence can always be checked later by inspecting the value of iter).

If models are not converging, increasing max.iter may not be the most efficient way to correct this problem. Consider increasing n.lambda or lambda.min in addition to increasing max.iter.

Although grpreg allows groups to be unordered and given arbitary names, it is recommended that you specify groups as consecutive integers. The first reason is efficiency: if groups are out of order, X must be reordered prior to fitting, then this process reversed to return coefficients according to the original order of X. This is inefficient if X is very large. The second reason is ambiguity with respect to other arguments such as group.multiplier. With consecutive integers, group=3 unambiguously denotes the third element of group.multiplier.

Seemingly unrelated regressions/multitask learning can be carried out using grpreg by passing a matrix to y. In this case, X will be used in separate regressions for each column of y, with the coefficients grouped across the responses. In other words, each column of X will form a group with m members, where m is the number of columns of y. For multiple Gaussian responses, it is recommended to standardize the columns of y prior to fitting, in order to apply the penalization equally across columns.

grpreg requires groups to be non-overlapping.

## Value

An object with S3 class "grpreg" containing:

**beta** The fitted matrix of coefficients. The number of rows is equal to the number of coefficients, and the number of columns is equal to nlambda.

family Same as above.

group Same as above.

lambda The sequence of lambda values in the path.

alpha Same as above.

deviance A vector containing the deviance of the fitted model at each value of lambda.

n Number of observations.

penalty Same as above.

**df** A vector of length nlambda containing estimates of effective number of model parameters all the points along the regularization path. For details on how this is calculated, see Breheny and Huang (2009).

**iter** A vector of length nlambda containing the number of iterations until convergence at each value of lambda.

**group.multiplier** A named vector containing the multiplicative constant applied to each group's penalty.

#### Author(s)

Patrick Breheny

#### References

- Breheny P and Huang J. (2009) Penalized methods for bi-level variable selection. *Statistics and its interface*, **2**: 369-380. doi:10.4310/sii.2009.v2.n3.a10
- Huang J, Breheny P, and Ma S. (2012). A selective review of group selection in high dimensional models. *Statistical Science*, **27**: 481-499. doi:10.1214/12sts392
- Breheny P and Huang J. (2015) Group descent algorithms for nonconvex penalized linear and logistic regression models with grouped predictors. *Statistics and Computing*, **25**: 173-187. doi:10.1007/s1122201394242
- Breheny P. (2015) The group exponential lasso for bi-level variable selection. *Biometrics*, **71**: 731-740. doi:10.1111/biom.12300

#### See Also

```
cv.grpreg(), as well as plot.grpreg() and select.grpreg() methods.
```

```
# Birthweight data
data(Birthwt)
X <- Birthwt$X
group <- Birthwt$group</pre>
# Linear regression
y <- Birthwt$bwt
fit <- grpreg(X, y, group, penalty="grLasso")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="grMCP")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="grSCAD")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="gel")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="cMCP")</pre>
plot(fit)
select(fit, "AIC")
# Logistic regression
y <- Birthwt$low
fit <- grpreg(X, y, group, penalty="grLasso", family="binomial")</pre>
plot(fit)
```

```
fit <- grpreg(X, y, group, penalty="grMCP", family="binomial")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="grSCAD", family="binomial")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="gel", family="binomial")</pre>
plot(fit)
fit <- grpreg(X, y, group, penalty="cMCP", family="binomial")</pre>
plot(fit)
select(fit, "BIC")
# Multitask learning (simulated example)
set.seed(1)
n <- 50
p <- 10
k <- 5
X <- matrix(runif(n*p), n, p)</pre>
y \leftarrow matrix(rnorm(n*k, X[,1] + X[,2]), n, k)
fit <- grpreg(X, y)</pre>
# Note that group is set up automatically
fit$group
plot(fit)
```

grpsurv

Fit an group penalized survival model

## **Description**

Fit regularization paths for Cox models with grouped penalties over a grid of values for the regularization parameter lambda.

## Usage

```
grpsurv(
 Χ,
  у,
  group = 1:ncol(X),
  penalty = c("grLasso", "grMCP", "grSCAD", "gel", "cMCP"),
  gamma = ifelse(penalty == "grSCAD", 4, 3),
  alpha = 1,
  nlambda = 100,
  lambda,
  lambda.min = {
     if (nrow(X) > ncol(X))
         0.001
     else 0.05
 },
 eps = 0.001,
 max.iter = 10000,
 dfmax = p,
```

```
gmax = length(unique(group)),
tau = 1/3,
group.multiplier,
warn = TRUE,
returnX = FALSE,
...
)
```

#### **Arguments**

X The design matrix.

y The time-to-event outcome, as a two-column matrix or Surv object. The first column should be time on study (follow up time); the second column should be

a binary variable with 1 indicating that the event has occurred and 0 indicating

(right) censoring.

group A vector describing the grouping of the coefficients. For greatest efficiency and

least ambiguity (see details), it is best if group is a factor or vector of consecutive integers, although unordered groups and character vectors are also allowed. If there are coefficients to be included in the model without being penalized, assign

them to group 0 (or "0").

penalty The penalty to be applied to the model. For group selection, one of grLasso,

grMCP, or grSCAD. For bi-level selection, one of gel or cMCP. See below for

details.

gamma Tuning parameter of the group or composite MCP/SCAD penalty (see details).

Default is 3 for MCP and 4 for SCAD.

alpha grpsurv allows for both a group penalty and an L2 (ridge) penalty; alpha con-

trols the proportional weight of the regularization parameters of these two penalties. The group penalties' regularization parameter is lambda\*alpha, while the regularization parameter of the ridge penalty is lambda\*(1-alpha). Default is

1: no ridge penalty.

nlambda The number of lambda values. Default is 100.

lambda A user-specified sequence of lambda values. By default, a sequence of values of

length nlambda is computed automatically, equally spaced on the log scale.

lambda.min The smallest value for lambda, as a fraction of lambda.max. Default is .001

if the number of observations is larger than the number of covariates and .05

otherwise.

eps Convergence threshhold. The algorithm iterates until the RMSD for the change

in linear predictors for each coefficient is less than eps. Default is 0.001.

max.iter Maximum number of iterations (total across entire path). Default is 10000.

dfmax Limit on the number of parameters allowed to be nonzero. If this limit is ex-

ceeded, the algorithm will exit early from the regularization path.

gmax Limit on the number of groups allowed to have nonzero elements. If this limit

is exceeded, the algorithm will exit early from the regularization path.

tau Tuning parameter for the group exponential lasso; defaults to 1/3.

group.multiplier

A vector of values representing multiplicative factors by which each group's penalty is to be multiplied. Often, this is a function (such as the square root) of the number of predictors in each group. The default is to use the square root of group size for the group selection methods, and a vector of 1's (i.e., no

adjustment for group size) for bi-level selection.

warn Return warning messages for failures to converge and model saturation? Default

is TRUE.

Return the standardized design matrix? Default is FALSE. returnX

#### **Details**

The sequence of models indexed by the regularization parameter lambda is fit using a coordinate descent algorithm. In order to accomplish this, the second derivative (Hessian) of the Cox partial log-likelihood is diagonalized (see references for details). The objective function is defined to be

$$Q(\beta|X,y) = \frac{1}{n}L(\beta|X,y) + P_{\lambda}(\beta)$$

where the loss function L is the negative partial log-likelihood (half the deviance) from the Cox regression model. See here for more details.

Presently, ties are not handled by grpsury in a particularly sophisticated manner. This will be improved upon in a future release of grpreg.

#### Value

An object with S3 class "grpsurv" containing:

beta The fitted matrix of coefficients. The number of rows is equal to the number of

coefficients, and the number of columns is equal to nlambda.

Same as above. group

lambda The sequence of lambda values in the path.

penalty Same as above. gamma Same as above. alpha Same as above.

deviance The deviance of the fitted model at each value of lambda.

The number of observations. n

df A vector of length nlambda containing estimates of effective number of model

parameters all the points along the regularization path. For details on how this

is calculated, see Breheny and Huang (2009).

iter A vector of length nlambda containing the number of iterations until conver-

gence at each value of lambda.

```
group.multiplier
```

A named vector containing the multiplicative constant applied to each group's penalty.

For Cox models, the following objects are also returned (and are necessary to estimate baseline survival conditional on the estimated regression coefficients), all of which are ordered by time on study (i.e., the ith row of W does not correspond to the ith row of X):

W Matrix of exp(beta) values for each subject over all lambda values.

time Times on study.

fail Failure event indicator.

#### Author(s)

Patrick Breheny

#### References

- Breheny P and Huang J. (2009) Penalized methods for bi-level variable selection. *Statistics and its interface*, **2**: 369-380. doi:10.4310/sii.2009.v2.n3.a10
- Huang J, Breheny P, and Ma S. (2012). A selective review of group selection in high dimensional models. *Statistical Science*, **27**: 481-499. doi:10.1214/12sts392
- Breheny P and Huang J. (2015) Group descent algorithms for nonconvex penalized linear and logistic regression models with grouped predictors. *Statistics and Computing*, **25**: 173-187. doi:10.1007/s1122201394242
- Breheny P. (2015) The group exponential lasso for bi-level variable selection. *Biometrics*, **71**: 731-740. doi:10.1111/biom.12300
- Simon N, Friedman JH, Hastie T, and Tibshirani R. (2011) Regularization Paths for Cox's Proportional Hazards Model via Coordinate Descent. *Journal of Statistical Software*, **39**: 1-13. doi:10.18637/jss.v039.i05

#### See Also

```
plot.grpreg(), predict.grpsurv(), cv.grpsurv()
```

```
data(Lung)
X <- Lung$X
y <- Lung$y
group <- Lung$group

fit <- grpsurv(X, y, group)
plot(fit)

S <- predict(fit, X, type='survival', lambda=0.05)
plot(S, xlim=c(0,200))</pre>
```

logLik.grpreg 21

logLik.grpreg	logLik method for grpreg	

## Description

Calculates the log likelihood and degrees of freedom for a fitted grpreg object.

#### Usage

```
## S3 method for class 'grpreg'
logLik(object, df.method = c("default", "active"), REML = FALSE, ...)
## S3 method for class 'grpsurv'
logLik(object, df.method = c("default", "active"), ...)
```

## **Arguments**

object	A fitted grpreg or grpsurv object, as obtained from grpreg() or grpsurv()
df.method	How should effective model parameters be calculated? One of: "active", which counts the number of nonzero coefficients; or "default", which uses the calculated df returned by grpreg. Default is "default".
REML	Use restricted MLE for estimation of the scale parameter in a gaussian model? Default is FALSE.
	For S3 method compatibility.

## **Details**

Exists mainly for use with stats::AIC() and stats::BIC().

#### Value

Returns an object of class 'logLik', in this case consisting of a number (or vector of numbers) with two attributes: 'df' (the estimated degrees of freedom in the model) and 'nobs' (number of observations).

The 'print' method for 'logLik' objects is not intended to handle vectors; consequently, the value of the function does not necessarily display correctly. However, it works with 'AIC' and 'BIC' without any glitches and returns the expected vectorized output.

## Author(s)

Patrick Breheny

#### See Also

```
grpreg()
```

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#### **Examples**

```
data(Birthwt)
X <- Birthwt$X
y <- Birthwt$bwt
group <- Birthwt$group
fit <- grpreg(X,y,group,penalty="cMCP")
logLik(fit) ## Display is glitchy for vectors
AIC(fit)
BIC(fit)</pre>
```

Lung

VA lung cancer data set

#### **Description**

Data from a randomised trial of two treatment regimens for lung cancer. This is a standard survival analysis data set from the classic textbook by Kalbfleisch and Prentice.

#### Usage

Lung

## **Format**

A list of two objects: y and X

- y A two column matrix (Surv object) containing the follow-up time (in days) and an indicator variable for whether the patient died while on the study or not.
- **X** A matrix with 137 observations (rows) and 9 predictor variables (columns). The remainder of this list describes the columns of X

**trt** Treatment indicator (1=control group, 2=treatment group)

karno Karnofsky performance score (0=bad, 100=good)

diagtime Time from diagnosis to randomization (months)

**age** Age (years, at baseline)

**prior** Prior therapy (0=no, 1=yes)

**squamous** Indicator for whether the cancer type is squamous cell carcinoma (0=no, 1=yes)

**small** Indicator for whether the cancer type is small cell lung cancer (0=no, 1=yes)

**adeno** Indicator for whether the cancer type is adenocarcinoma (0=no, 1=yes)

**large** Indicator for whether the cancer type is large cell carcinoma (0=no, 1=yes)

#### Source

```
https://cran.r-project.org/package=survival
```

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#### References

 Kalbfleisch D and Prentice RL (1980), The Statistical Analysis of Failure Time Data. Wiley, New York.

#### See Also

```
grpsurv()
```

plot.cv.grpreg

Plots the cross-validation curve from a cv.grpreg object

#### **Description**

Plots the cross-validation curve from a cv. grpreg object, along with standard error bars.

#### Usage

```
## S3 method for class 'cv.grpreg'
plot(
    x,
    log.l = TRUE,
    type = c("cve", "rsq", "scale", "snr", "pred", "all"),
    selected = TRUE,
    vertical.line = TRUE,
    col = "red",
    ...
)
```

## Arguments

Χ		A cv	grpr'.grpr	-eg	objec	t.
-	-	~1				

log.1 Should horizontal axis be on the log scale? Default is TRUE.

What to plot on the vertical axis. cve plots the cross-validation error (deviance); rsq plots an estimate of the fraction of the deviance explained by the model (R-squared); snr plots an estimate of the signal-to-noise ratio; scale plots, for family="gaussian", an estimate of the scale parameter (standard deviation); pred plots, for family="binomial", the estimated prediction error; all pro-

duces all of the above.

selected If TRUE (the default), places an axis on top of the plot denoting the number of

groups in the model (i.e., that contain a nonzero regression coefficient) at that

value of lambda.

vertical.line If TRUE (the default), draws a vertical line at the value where cross-validaton

error is minimized.

col Controls the color of the dots (CV estimates).

... Other graphical parameters to plot

plot.grpreg

#### **Details**

Error bars representing approximate +/- 1 SE (68\ plotted along with the estimates at value of lambda. For rsq and snr, these confidence intervals are quite crude, especially near zero, and will hopefully be improved upon in later versions of grpreg.

## See Also

```
grpreg(), cv.grpreg()
```

### **Examples**

```
# Birthweight data
data(Birthwt)
X <- Birthwt$X
group <- Birthwt$group</pre>
# Linear regression
y <- Birthwt$bwt
cvfit <- cv.grpreg(X, y, group)</pre>
plot(cvfit)
op <- par(mfrow=c(2,2))
plot(cvfit, type="all")
## Logistic regression
y <- Birthwt$low
cvfit <- cv.grpreg(X, y, group, family="binomial")</pre>
par(op)
plot(cvfit)
par(mfrow=c(2,2))
plot(cvfit, type="all")
```

plot.grpreg

Plot coefficients from a "grpreg" object

## Description

Produces a plot of the coefficient paths for a fitted grpreg object.

#### Usage

```
## S3 method for class 'grpreg'
plot(x, alpha = 1, legend.loc, label = FALSE, log.l = FALSE, norm = FALSE, ...)
```

#### **Arguments**

```
x Fitted "grpreg" model.alpha Controls alpha-blending. Default is alpha=1.
```

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legend.loc	Where should the legend go? If left unspecified, no legend is drawn. See legend for details.
label	If TRUE, annotates the plot with text labels in the right margin describing which variable/group the corresponding line belongs to.
log.l	Should horizontal axis be on the log scale? Default is FALSE.
norm	If TRUE, plot the norm of each group, rather than the individual coefficients.
	Other graphical parameters to plot, matlines, or legend

#### See Also

```
grpreg()
```

## **Examples**

```
# Fit model to birthweight data
data(Birthwt)
X <- Birthwt$X</pre>
y <- Birthwt$bwt
group <- Birthwt$group</pre>
fit <- grpreg(X, y, group, penalty="grLasso")</pre>
# Plot (basic)
plot(fit)
# Plot group norms, with labels in right margin
plot(fit, norm=TRUE, label=TRUE)
# Plot (miscellaneous options)
myColors <- c("black", "red", "green", "blue", "yellow", "purple",</pre>
"orange", "brown")
plot(fit, legend.loc="topleft", col=myColors)
plot(fit, legend.loc="topleft", lwd=6, alpha=0.5, legend=labs)
plot(fit, norm=TRUE, legend.loc="topleft", lwd=6, alpha=0.5, legend=labs)
```

plot.grpsurv.func

Plot survival curve for grpsurv model

## Description

Plot survival curve for a model that has been fit using grpsurv followed by a prediction of the survival function using predict.grpsurv

#### Usage

```
## S3 method for class 'grpsurv.func'
plot(x, alpha = 1, ...)
```

plot\_spline

## Arguments

X	A 'grpsurv.func' object, which is returned by predict.grpsurv if type='survival' is specified. See examples.
alpha	Controls alpha-blending (i.e., transparency). Useful if many overlapping lines are present.
	Other graphical parameters to pass to plot

## Author(s)

Patrick Breheny

#### See Also

```
grpsurv, predict.grpsurv
```

## **Examples**

```
data(Lung)
X <- Lung$X
y <- Lung$y
group <- Lung$group
fit <- grpsurv(X, y, group)

# A single survival curve
S <- predict(fit, X[1,], type='survival', lambda=.05)
plot(S, xlim=c(0,200))

# Lots of survival curves
S <- predict(fit, X, type='survival', lambda=.05)
plot(S, xlim=c(0,200), alpha=0.3)</pre>
```

plot\_spline

Plot spline curve for a fitted additive model

## **Description**

Plots a spline curve for a single variable using a grpreg or cv. grpreg object for which an additive model was fit.

## Usage

```
plot_spline(
   fit,
   variable,
   lambda,
   which = NULL,
   partial = FALSE,
```

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```
type = "contrast",
warnings = TRUE,
points.par = NULL,
add = FALSE,
...
)
```

#### **Arguments**

fit A grpreg object. The model must have been fit using a expand\_spline object. variable The name of the variable which will be plotted (character). lambda Values of the regularization parameter lambda which will be used for the plot. If a vector is passed, a curve will be drawn for each value of lambda (numeric vector; if a cv.grpreg object is passed, the lambda value minimizing crossvalidation error will be used as a default; otherwise, there is no default value) which Index of penalty parameter lambda which will be used for the plot. If both lambda and which are specified, lambda takes precedence (integer vector). If TRUE, a scatter plot of the partial residuals is superimposed on the curve (logipartial cal; default = FALSE). If multiple lambdas are specified, the largest value is used to calculate the residuals. Type of plot to be produced (default = "contrast"). The following options are type supported: • If "conditional", the plot returned shows the value of the variable on the x-axis and the change in linear predictor on the y-axis, holding all other variables constant at their mean value. • If "contrast", the plot returned shows the effect on the linear predictor by moving the x variable away from its mean. warnings If FALSE, warnings will be suppressed (default = TRUE). List of parameters (see par() to pass to points() when partial=TRUE. points.par add Add spline to existing plot? (default: FALSE) Further arguments to be passed to plot(). Note that these arguments also con-. . . trol the appearance of the lines.

#### **Details**

plot\_spline() takes a model fit using both the grpreg() and expand\_spline() functions and plots a spline curve for a given variable.

```
Data <- gen_nonlinear_data(n=1000)
X <- expand_spline(Data$X)
fit <- grpreg(X, Data$y)
plot_spline(fit, "V02", lambda = 0.03)
plot_spline(fit, "V02", which = c(10, 90))
plot_spline(fit, "V02", lambda = 0.03, partial=TRUE)</pre>
```

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predict.cv.grpreg

Model predictions based on a fitted grpreg object

## Description

Similar to other predict methods, this function returns predictions from a fitted "grpreg" object.

## Usage

```
## S3 method for class 'cv.grpreg'
predict(
  object,
  Χ,
  lambda = object$lambda.min,
 which = object$min,
 type = c("link", "response", "class", "coefficients", "vars", "groups", "nvars",
    "ngroups", "norm"),
)
## S3 method for class 'cv.grpreg'
coef(object, lambda = object$lambda.min, which = object$min, ...)
## S3 method for class 'grpreg'
predict(
 object,
 type = c("link", "response", "class", "coefficients", "vars", "groups", "nvars",
    "ngroups", "norm"),
  lambda,
 which = 1:length(object$lambda),
)
## S3 method for class 'grpreg'
coef(object, lambda, which = 1:length(object$lambda), drop = TRUE, ...)
```

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#### **Arguments**

object	Fitted "grpreg" or "cv.grpreg" model object.
Χ	Matrix of values at which predictions are to be made. Not used for type="coefficients"
lambda	Values of the regularization parameter lambda at which predictions are requested. For values of lambda not in the sequence of fitted models, linear interpolation is used.
which	Indices of the penalty parameter lambda at which predictions are required. By default, all indices are returned. If lambda is specified, this will override which.
type	Type of prediction: "link" returns the linear predictors; "response" gives the fitted values; "class" returns the binomial outcome with the highest probability; "coefficients" returns the coefficients; "vars" returns the indices for the nonzero coefficients; "groups" returns the indices for the groups with at least one nonzero coefficient; "nvars" returns the number of nonzero coefficients; "ngroups" returns the number of groups with at least one nonzero coefficient; "norm" returns the L2 norm of the coefficients in each group.
	Not used.

By default, if a single value of lambda is supplied, a vector of coefficients is

returned. Set drop=FALSE if you wish to have coef always return a matrix (see

#### **Details**

drop

coef and predict methods are provided for "cv.grpreg" options as a convenience. They simply call coef.grpreg and predict.grpreg with lambda set to the value that minimizes the cross-validation error.

#### Value

The object returned depends on type.

drop).

## Author(s)

Patrick Breheny

## See Also

grpreg

```
# Fit penalized logistic regression model to birthweight data
data(Birthwt)
X <- Birthwt$X
y <- Birthwt$low
group <- Birthwt$group
fit <- grpreg(X, y, group, penalty="grLasso", family="binomial")
# Coef and predict methods</pre>
```

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```
coef(fit, lambda=.001)
predict(fit, X, type="link", lambda=.07)[1:10]
predict(fit, X, type="response", lambda=.07)[1:10]
predict(fit, X, type="class", lambda=.01)[1:15]
predict(fit, type="vars", lambda=.07)
predict(fit, type="groups", lambda=.07)
predict(fit, type="norm", lambda=.07)

# Coef and predict methods for cross-validation
cvfit <- cv.grpreg(X, y, group, family="binomial", penalty="grMCP")
coef(cvfit)
predict(cvfit, X)[1:10]
predict(cvfit, X, type="response")[1:10]
predict(cvfit, type="groups")</pre>
```

predict.grpsurv

Model predictions for grpsurv objects

## **Description**

Similar to other predict methods, this function returns predictions from a fitted grpsurv object.

### Usage

### **Arguments**

object Fitted grpsurv model object.

X Matrix of values at which predictions are to be made. Not required for some

type values.

type Type of prediction:

• link: linear predictors

• response: risk (i.e., exp(link))

• survival: the estimated survival function

• hazard: the estimated cumulative hazard function

• median: median survival time

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	<ul> <li>The other options are all identical to their grpreg() counterparts</li> </ul>
lambda	Regularization parameter at which predictions are requested. For values of lambda not in the sequence of fitted models, linear interpolation is used.
which	Indices of the penalty parameter lambda at which predictions are required. Default: all indices. If lambda is specified, this will override which.
	Not used.

#### **Details**

Estimation of baseline survival function conditional on the estimated values of beta is carried out according to the method described in Chapter 4.3 of Kalbfleisch and Prentice.

#### Value

The object returned depends on type.

## Author(s)

Patrick Breheny

#### References

• Kalbfleish JD and Prentice RL (2002). The Statistical Analysis of Failure Time Data, 2nd edition. Wiley.

#### See Also

```
grpsurv()
```

```
data(Lung)
X <- Lung$X
y <- Lung$y
group <- Lung$group</pre>
fit <- grpsurv(X, y, group)</pre>
coef(fit, lambda=0.05)
head(predict(fit, X, type="link", lambda=0.05))
head(predict(fit, X, type="response", lambda=0.05))
# Survival function
S <- predict(fit, X[1,], type="survival", lambda=0.05)
S(100)
S <- predict(fit, X, type="survival", lambda=0.05)</pre>
plot(S, xlim=c(0,200))
# Medians
predict(fit, X[1,], type="median", lambda=0.05)
M <- predict(fit, X, type="median")</pre>
```

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```
M[1:10, 1:10]
# Nonzero coefficients
predict(fit, type="vars", lambda=c(0.1, 0.01))
predict(fit, type="nvars", lambda=c(0.1, 0.01))
```

residuals.grpreg

Extract residuals from a grpreg or grpsurv fit

## Description

Currently, only deviance residuals are supported.

## Usage

```
## S3 method for class 'grpreg'
residuals(object, lambda, which = 1:length(object$lambda), drop = TRUE, ...)
```

## Arguments

object	Object of class grpreg or grpsurv.
lambda	Values of the regularization parameter at which residuals are requested (numeric vector). For values of lambda not in the sequence of fitted models, linear interpolation is used.
which	Index of the penalty parameter at which residuals are requested (default = all indices). If lambda is specified, this take precedence over which.
drop	By default, if a single value of lambda is supplied, a vector of residuals is returned (logical; default=TRUE). Set drop=FALSE if you wish to have the function always return a matrix (see drop()).
	Not used.

```
data(Birthwt)
X <- Birthwt$X
y <- Birthwt$bwt
group <- Birthwt$group
fit <- grpreg(X, y, group, returnX=TRUE)
residuals(fit)[1:5, 1:5]
head(residuals(fit, lambda=0.1))</pre>
```

select 33

select

Select an value of lambda along a grpreg path

### **Description**

Selects a point along the regularization path of a fitted grpreg object according to the AIC, BIC, or GCV criteria.

### Usage

```
select(obj, ...)
## S3 method for class 'grpreg'
select(
  obj,
  criterion = c("BIC", "AIC", "GCV", "AICc", "EBIC"),
  df.method = c("default", "active"),
  smooth = FALSE,
  ...
)
```

#### **Arguments**

obj A fitted grpreg object.

... For S3 method compatibility.

criterion The criterion by which to select the regularization parameter. One of "AIC", "BIC", "GCV", "AICc", or "EBIC"; default is "BIC".

df.method How should effective model parameters be calculated? One of: "active", which counts the number of nonzero coefficients; or "default", which uses the calculated df returned by grpreg. Default is "default".

smooth Applies a smoother to the information criteria before selecting the optimal value.

#### **Details**

The criteria are defined as follows, where L is the deviance (i.e, -2 times the log-likelihood),  $\nu$  is the degrees of freedom, and n is the sample size:

$$AIC = L + 2\nu$$
 
$$BIC = L + \log(n)\nu$$
 
$$GCV = \frac{L}{(1 - \nu/n)^2}$$
 
$$AICc = AIC + 2\frac{\nu(\nu + 1)}{n - \nu - 1}$$
 
$$EBIC = BIC + 2\log\binom{p}{\nu}$$

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#### Value

A list containing:

lambda The selected value of the regularization parameter, lambda.

beta The vector of coefficients at the chosen value of lambda.

**df** The effective number of model parameters at the chosen value of lambda.

IC A vector of the calculated model selection criteria for each point on the regularization path.

#### See Also

```
grpreg()
```

## **Examples**

```
data(Birthwt)
X <- Birthwt$X
y <- Birthwt$bwt
group <- Birthwt$group
fit <- grpreg(X, y, group, penalty="grLasso")
select(fit)
select(fit,crit="AIC",df="active")
plot(fit)
abline(v=select(fit)$lambda)
par(mfrow=c(1,3))
1 <- fit$lambda
xlim <- rev(range(l))
plot(l, select(fit)$IC, xlim=xlim, pch=19, type="o", ylab="BIC")
plot(l, select(fit,"AIC")$IC, xlim=xlim, pch=19, type="o",ylab="AIC")
plot(l, select(fit,"GCV")$IC, xlim=xlim, pch=19, type="o",ylab="GCV")</pre>
```

summary.cv.grpreg

Summarizing inferences based on cross-validation

## **Description**

Summary method for cv.grpreg or cv.grpsurv objects

### Usage

```
## S3 method for class 'cv.grpreg'
summary(object, ...)
## S3 method for class 'summary.cv.grpreg'
print(x, digits, ...)
```

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#### **Arguments**

object A "cv.grpreg" object.

... Further arguments passed to or from other methods.

x A "summary.cv.grpreg" object.

digits Number of digits past the decimal point to print out. Can be a vector specifying

different display digits for each of the five non-integer printed values.

#### Value

summary(cvfit) produces an object with S3 class "summary.cv.grpreg". The class has its own print method and contains the following list elements:

penalty The penalty used by grpreg/grpsurv.

model The type of model: "linear", "logistic", "Poisson", "Cox", etc.

n Number of observations

p Number of regression coefficients (not including the intercept).

min The index of lambda with the smallest cross-validation error.

lambda The sequence of lambda values used by cv.grpreg/cv.grpsurv.

cve Cross-validation error (deviance).

r.squared Proportion of variance explained by the model, as estimated by cross-validation.

snr Signal to noise ratio, as estimated by cross-validation.

sigma For linear regression models, the scale parameter estimate.

pe For logistic regression models, the prediction error (misclassification error).

#### Author(s)

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#### See Also

```
grpreg, cv.grpreg, cv.grpsurv, plot.cv.grpreg
```

```
# Birthweight data
data(Birthwt)
X <- Birthwt$X
group <- Birthwt$group

# Linear regression
y <- Birthwt$bwt
cvfit <- cv.grpreg(X, y, group)
summary(cvfit)

# Logistic regression
y <- Birthwt$low</pre>
```

36 summary.cv.grpreg

```
cvfit <- cv.grpreg(X, y, group, family="binomial")
summary(cvfit)

# Cox regression
data(Lung)
cvfit <- with(Lung, cv.grpsurv(X, y, group))
summary(cvfit)</pre>
```

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