

Package ‘iGraphMatch’

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Type Package

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Description

Versatile tools and data for graph matching analysis with various forms of prior information that supports working with 'igraph' objects, matrix objects, or lists of either.

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<https://rdrr.io/github/dpmcsuss/iGraphMatch/>

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best_matches	<i>Rank best matches</i>
--------------	--------------------------

Description

Rank vertex-pairs in order of a goodness of matching metric

Usage

```
best_matches(A, B, match, measure, num = NULL, true_label = NULL)
```

Arguments

A	A matrix, an igraph object, or a list of either. See check_graph
B	A matrix, an igraph object, or a list of either. See check_graph
match	graphMatch , eg result of call to gm
measure	One of "row_cor", "row_diff", or "row_perm_stat" or a function (see details). Measure for computing goodness of matching.

num A positive integer or NULL. Number of pairs of best matched vertices needed. NULL indicates all matches.

true_label the true correspondence (if available).

Details

If measure is a function, it should take exactly two matrices or igraph objects as arguments and return a vector of length equal to the number of nonseed nodes in the first object. Smaller values will be taken to indicate better matches.

Value

best_matches returns a data frame with the indices of best matched vertices in G_1 named A_best, the indices of best matched vertices in G_2 named B_best and the values of measure for best matches, where smaller values indicate better matches for all measures. If the true correspondence is available, also returns the precision of top n best matches, for each $n \leq \text{num}$.

row_cor takes 1 minus the row correlation value for the corresponding vertex. row_diff takes the row difference value for each corresponding vertex. row_perm_stat uses the row permutation statistics value.

Examples

```
cgnp_pair <- sample_correlated_gnp_pair(n = 50, corr = 0.5, p = 0.5)
g1 <- cgnp_pair$graph1
g2 <- cgnp_pair$graph2
seeds <- 1:50 <= 10
match <- gm(g1, g2, seeds, method = "indefinite")

# Application: select best matched seeds from non seeds as new seeds, and do the
# graph matching iteratively to get higher matching accuracy
best_matches(A = g1, B = g2, match = match, measure = "row_perm_stat", num = 5, true_label = 1:50)
```

C.Elegans

Chemical synapses and electrical synapses networks of roundworm

Description

C.Elegans networks consist of the chemical synapses network and the electrical synapses network of the roundworm, where each of 279 nodes represents a neuron and each edge represents the intensity of synapses connections between two neurons.

Usage

```
data(C.Elegans)
```

Format

An object of class `list` of length 2.

Details

Two networks are weighted and directed graphs with self-loops. There are 2194 and 1031 edges in two graphs respectively and the empirical Pearson's correlation between two graphs is 0.17. Two networks are stored in a list in the form of `igraph` objects, where the first network in the list is the chemical synapses network and the other one is the electrical synapses network.

References

Chen, L., Vogelstein, J. T., Lyzinski, V., & Priebe, C. E. (2016). *A joint graph inference case study: the C. elegans chemical and electrical connectomes*. *Worm*, 5(2), e1142041.

Sulston, J. E., Schierenberg, E., White, J. G., & Thomson, J.N. (1983). *The embryonic cell lineage of the nematode caenorhabditis elegans*. *Developmental biology*, 100(1):64–119.

Examples

```
data(C.Elegans)
g1 <- C.Elegans[[1]]
g2 <- C.Elegans[[2]]
plot(g1, g2)
```

center_graph

Center adjacency matrix

Description

Center the adjacency matrix by re-weighting edges according to a specified scheme

Usage

```
center_graph(A, scheme = c(-1, 1), use_splr = TRUE)
```

Arguments

<code>A</code>	A matrix, an <code>igraph</code> object. Adjacency matrix.
<code>scheme</code>	A character vector, number or pair of numbers. Default <code>c(-1, 1)</code> . See Details.
<code>use_splr</code>	A boolean indicating whether to use the splrMatrix object when storing the centered graph. Defaults to <code>TRUE</code> .

Details

The options for scheme are

- "naive" Returns original A
- Integer: Returns $A - A_{scheme}$ where A_{scheme} is the best rank-scheme approximation of A.
- A pair of scalars: Returns $s * A + a$ such that the minimum of the returned matrix is $\min(\text{scheme})$ and the maximum is $\max(\text{scheme})$.
- "center": Same as $\text{scheme} = c(-1, 1)$

Value

centered adjacency matrix as a [splrMatrix](#) if `useSplr = TRUE`, otherwise as a `Matrix` object.

Examples

```
A <- sample_correlated_gnp_pair(n = 10, corr = .5, p = .5)$graph1
center_graph(A, scheme = "naive")
center_graph(A, scheme = "center")
center_graph(A, scheme = 2)
center_graph(A, scheme = c(-4, 2))
```

check_graph

Parameter checking for a graph-pair

Description

Function that checks that the pair of graphs passed to a matching-related functions satisfies necessary conditions and modifies them according to specified parameters. `check_single_graph` does similar checks and modifications but just for one graph or list of graphs.

Usage

```
check_graph(
  A,
  B,
  same_order = TRUE,
  square = TRUE,
  as_list = TRUE,
  as_igraph = FALSE
)

check_single_graph(A, square = TRUE, as_list = TRUE, as_igraph = FALSE)
```

Arguments

A	A matrix, an igraph object, or list of either.
B	A matrix, an igraph object, or list of either.
same_order	Whether the returned objects should have the same number of nodes. If the graphs start with different numbers of nodes the smaller graph is padded with isolated vertices. (default = TRUE)
square	Whether the matrices need to be square. (default = TRUE) Currently non-square matrices are not supported.
as_list	Whether to return the results as a matrix_list. (default = TRUE) If FALSE and A and B have length > 1
as_igraph	Whether to return an igraph object. (default=FALSE) Only allowed if the original parameters are igraph objects. If FALSE, then this converts the objects to sparse matrices.

Details

If A and B are lists of matrices or igraph objects, then the lists must be the same length. Additionally, within each list the graphs need to have the same number of vertices but this does not need to be true across lists.

Value

List containing A and B modified according to the parameters and the number of vertices in each graph in totv1 and totv2.

check_seeds	<i>Standardize seeds input data type</i>
-------------	--

Description

Convert the input seeds data into data frame type with the first column being the indices of G_1 and the second column being the corresponding indices of G_2

Usage

```
check_seeds(seeds, nv, logical = FALSE)
```

Arguments

seeds	A vector of integers or logicals, a matrix or a data frame. Input in the form of a vector of integers denotes the indices of seeds which are identical in both graphs. Input in the form of a vector of logicals indicate the location of seeds with TRUE and the indices of seeds are identical in both graphs. Input in the form of a matrix or a data frame, with the first column being the indices of G_1 and the second column being the corresponding indices of G_2 .
-------	---

nv	An integer. Number of total vertices.
logical	A logical. TRUE indicates to return seeds in a vector of logicals where TRUE indicates the corresponding vertex is a seed. FALSE indicates to return a data frame.

Value

returns a data frame with the first column being the corresponding indices of G_1 and the second column being the corresponding indices of G_2 or a vector of logicals where TRUE indicates the corresponding vertex is a seed.

Examples

```
#input is a vector of logicals
check_seeds(1:10 <= 3, nv = 10)

#input is a vector of integers
check_seeds(c(1,4,2,7,3), nv = 10)

#input is a matrix
check_seeds(matrix(1:4,2), nv = 10)

#input is a data frame
check_seeds(as.data.frame(matrix(1:4,2)), nv = 10)
```

check_sim	<i>Check the similarity matrix passed to a matching function</i>
-----------	--

Description

Internal function that checks that a similarity matrix satisfies necessary conditions and modifies it for use in graph matching.

Usage

```
check_sim(sim, seeds, nonseeds, totv1, totv2, for_nonseeds = TRUE)
```

Arguments

sim	Similarity matrix
seeds	dataframe of seed matches from running check_seeds
nonseeds	dataframe of nonseed nodes from running check_seeds
totv1	total number of vertices in the first graph
totv2	total number of vertices in the second graph
for_nonseeds	Whether the similarities are between non-seed nodes only (default = TRUE), or if similarities among seed nodes are included (FALSE)

Details

The goal here is to be flexible in terms of the dimensions of the similarity matrix passed to `gm`. This is useful when the graphs have different orders in which case the function accepts matrices with dimensions equal to that of orders of the original graphs or the number of nonseeds.

Value

Standardized similarity matrix for similarities only between nonseeds across the two graphs, if `for_nonseeds = TRUE`, or between all nodes, if `for_nonseeds = FALSE`

<code>do_lap</code>	<i>Linear (sum) assignment problem</i>
---------------------	--

Description

Compute the best bipartite matching using one of three methods. For an $n \times n$ score matrix it find $\max_{v \in \Pi_n} \sum_{i=1}^n score_{i,v(i)}$ where Π_n denotes all permutations on n objects.

Usage

```
do_lap(score, method = "clue")
```

Arguments

score	matrix of pairwise scores
method	One of "lapjv", "lapmod", or "clue"

Details

Solves a linear assignment using one of three methods. "clue" uses `solve_lsap` from the `clue` package. "lapjv" uses the Jonker-Volgenant approach implemented in this package. "lapmod" use a modification of JV that exploits sparsity in the score matrix.

Scores do not need to be non-negative. For "clue" the scores are pre-translated to be non-negative which preserves the LAP solution.

Value

`do_lap` returns a vector which indicates the best matching column for each row.

References

- R. Jonker, A. Volgenant (1987). *A shortest augmenting path algorithm for dense and sparse linear assignment problems*. Computing, pages 325-340.
- A. Volgenant (1996). *Linear and Semi-Assignment Problems: A Core Oriented Approach*. Computer Ops Res., pages 917-932.
- C. H. Papadimitriou and K. Steiglitz (1998). *Combinatorial Optimization: Algorithms and Complexity*. Courier Corporation.

Examples

```
set.seed(12345)
cost <- Matrix::rsparsematrix(10, 10, .5)
cbind(
  do_lap(cost, "lapjv"),
  do_lap(cost, "lapmod"),
  do_lap(cost, "clue")
)
```

Enron

Email communication networks of Enron Corporation

Description

The Enron network data consists of email messages between 184 employees of the Enron Corporation where each graph represents one week of emails and each edge indicates whether there is email sent from one employee to the other.

Usage

```
data(Enron)
```

Format

An object of class `list` of length 2.

Details

Two networks are unweighted and directed with self-loops. There are 488 and 482 edges in two networks respectively and the empirical Pearson's correlation between two graphs is 0.85. Two email communication networks for two different weeks are stored in a list in the form of `igraph` objects.

References

Originally released by William Cohen at CMU. [More details](#) on the origins and research uses of the dataset.

Examples

```
data(Enron)
g1 <- Enron[[1]]
g2 <- Enron[[2]]
plot(g1, g2)
```

get_perm_mat	<i>Get Permutation</i>
--------------	------------------------

Description

Get an m -by- n permutation matrix according to the mapping correspondence.

Usage

```
get_perm_mat(match, dim = NULL, padded = FALSE, seeds = TRUE)
```

Arguments

match	Either a graphMatch object or 2-column matrix or data frame. The first and second columns correspond to indices in G_1 and G_2 respectively.
dim	desired dimensions of the matrix. Note, this does not have to be square. If NULL and match is a graphMatch object then dim is set to dim(match)
padded	If FALSE then this returns a square matrix the size of the larger of the two graph otherwise dim = dim(match). This is ignored if match is not a graphMatch object.
seeds	Whether to keep the seed vertices (TRUE) from the match or to remove them (FALSE). Ignored if match is not a graphMatch object.

Value

get_perm_mat returns an m -by- n sparse permutation matrix or whose submatrix is a permutation matrix if only parts of nodes from both graphs get matched or in the case of matching graphs of different order.

Examples

```
# returns a permutation matrix: m=n, all the nodes get matched
corr <- data.frame(corr_A = c(1,2,3,4), corr_B = c(1,4,2,3))
get_perm_mat(corr, c(4, 4))

# submatrix is a permutation matrix: parts of graphs get matched
get_perm_mat(corr, c(5, 6))
```

Description

gm is used to match a pair of given graphs, with specifications of the adjacency matrices of for a pair of graphs, possible prior knowledge, and a graph matching method.

Usage

```
gm(A, B, seeds = NULL, similarity = NULL, method = "indefinite", ...)
```

Arguments

A	A matrix, igraph object, or list of either.
B	A matrix, igraph object, or list of either.
seeds	A vector of integers or logicals, a matrix or a data frame. If the seed pairs have the same indices in both graphs then seeds can be a vector. If not, seeds must be a matrix or a data frame, with the first column being the indices of G_1 and the second column being the corresponding indices of G_2 .
similarity	A matrix. An n-by-n matrix containing vertex similarities. Mandatory for the "IsoRank" method.
method	Choice for graph matching methods. One of "indefinite", "convex", "PATH", "percolation", "IsoRank", "Umeyama", or a user-defined graph matching function. Please check Details and Examples sections for instructions on how to define your own function.
...	Arguments passed to graph matching methods. Please refer to Details section for more information.

Details

If method is a function, it should take two matrices or igraph objects, seeds and similarity scores as arguments for minimum. Additionally, it can also take other arguments if needed. The self-defined function should return a graphMatch class object with matching correspondence, sizes of two input graphs, matching formula, and other algorithm hyperparameter details.

The method argument can also take one of the implemented algorithms, including ["indefinite"](#), ["convex"](#), ["PATH"](#), ["percolation"](#), ["IsoRank"](#), and ["Umeyama"](#). In this case, one can pass additional arguments to the gm function according to the specified method. For a detailed list of additional arguments for each one of the implemented method, please click on the corresponding method name for its help page.

Value

gm returns an object of class "[graphMatch](#)". See [graphMatch-class](#) and links therein for details on the graph match class.

Additionally, gm also returns a list of matching details of the specified method. Please refer to the help page for each implemented method, i.e. "[indefinite](#)", "[convex](#)", "[PATH](#)", "[percolation](#)", "[IsoRank](#)", and "[Umeyama](#)" for details on the corresponding returned list.

Examples

```
# match G_1 & G_2 with some known node pairs as seeds
set.seed(123)
cgnp_pair <- sample_correlated_gnp_pair(n = 10, corr = 0.5, p = 0.5)
g1 <- cgnp_pair$graph1
g2 <- cgnp_pair$graph2
seeds <- 1:10 <= 4

m_rds <- gm(g1, g2, seeds, method = "indefinite", start = "rds", max_iter = 20)
summary(m_rds, g1, g2, true_label = 1:10)

# match two multi-layer graphs
set.seed(123)
gp_list <- replicate(3, sample_correlated_gnp_pair(20, .3, .5), simplify = FALSE)
A <- lapply(gp_list, function(gp)gp[[1]])
B <- lapply(gp_list, function(gp)gp[[2]])

m_perco <- gm(A, B, seeds, method = "percolation", ExpandWhenStuck = FALSE)
summary(m_perco, A, B)

sim <- as.matrix(init_start(start = "bari", nns = 20, soft_seeds = 1:5))
m_Iso <- gm(A, B, similarity = sim, method = "IsoRank", lap_method = "greedy")
summary(m_Iso, A, B)

# customized graph matching algorithm
graph_match_rand <- function(A, B, seeds = NULL, similarity = NULL, rand_seed){
  nm <- min(nrow(A), nrow(B))
  set.seed(rand_seed)
  m <- data.frame(sample(nrow(A), nm), corr_B = sample(nrow(B), nm))
  m <- as.graphMatch(m)
  m$rand_seed <- rand_seed
  m
}

m_self <- gm(g1, g2, method = graph_match_rand, rand_seed = 123)
summary(m_self, g1, g2)
```

Description

An S4 class for the results of a graph matching function

Usage

```
graphMatch(corr, nnodes, call = NULL, detail = list())
```

```
as.graphMatch(from)
```

Arguments

corr	data.frame indicating the correspondence between two graphs
nnodes	dimensions of the original two graphs
call	The call to the graph matching function
detail	List with other more detailed information
from	object to convert to graphMatch object

Details

graphMatch objects are returned by any of the graph matching methods implemented in the iGraph-Match package. These objects are primarily to represent the found correspondence between the two vertex sets. This is represented by a data.frame with two columns indicating the aligned vertex-pairs across the two graphs.

Value

graphMatch object

Slots

corr	data.frame indicating the correspondence between two graphs
nnodes	of the original two graphs
call	The call to the graph matching function

See Also

[graphMatch_methods](#), [graphMatch_summary](#), [graphMatch_operators](#), [graphMatch_plot](#)

Examples

```
# sample a pair of correlated random graphs from G(n,p)
set.seed(123)
cgnp_pair <- sample_correlated_gnp_pair(n = 10, corr = 0.3, p = 0.5)
g1 <- cgnp_pair$graph1
g2 <- cgnp_pair$graph2

# match g1 & g2 using percolation algorithm with some known node pairs as seeds
match <- gm(A = g1, B = g2, seeds = 1:3, method = 'indefinite')
```

```

# graphMatch object
match

match$corr_A # matching correspondence in the first graph
match$corr_B # matching correspondence in the second graph
match$seeds # vector of logicals indicating seeded nodes

as.data.frame(match)
match[]
dim(match)
length(match)

# matching details unique to the FW methodology with indefinite relaxation
match$iter # number of iterations
match$soft # doubly stochastic matrix from the last iteration, can be used to extract soft matching
match$lap_method # method for solving lap

# create a graphMatch object from a data.frame or matrix
as.graphMatch(data.frame(1:5, 1:5))
as.graphMatch(1:5)

```

init_start

Initialization of the start matrix

Description

Initialize the start matrix for graph matching iteration.

Usage

```
init_start(start, nns, ns = 0, soft_seeds = NULL, seeds = NULL, ...)
```

Arguments

start	A matrix, character, or function. A <i>nns</i> -by- <i>nns</i> matrix, start method like "bari", "convex" or "rds", or a function to initialize the start matrix. If a function, it must have at least the arguments <i>nns</i> , <i>ns</i> , and <i>softs_seeds</i> .
nns	An integer. Number of non-seeds.
ns	An integer. Number of seeds.
soft_seeds	A vector, a matrix or a data frame indicating entries of the start matrix that will be initialized at 1 to indicate . See check_seeds .
seeds	A vector, a matrix or a data frame. Indicating hard seeds. These are used for "convex" start but otherwise are ignored.
...	Arguments passed to other start functions. See details in Values section.

Details

When `start` is a character, there are five options.

- "bari" initializes at the barycenter.
- "rds_perm_bari" gives a random linear combination of barycenter and a random permutation matrix, $(1-a)B + aP$. The argument `g` controls `a` with `a` being sampled as `g * runif()`.
- "rds" gives a random doubly stochastic matrix. Users can specify a random deviates generator to the `distribution` argument, and the default is `runif`. A random matrix with iid entries from `distribution` and the Sinkhorn algorithm is applied to produce the output.
- "rds_from_sim" gives a random doubly stochastic matrix derived from similarity scores. One needs to input a similarity score matrix to the `sim` argument for this method. The procedure is the same as "rds" but before the Sinkhorn algorithm is applied, the entries of the random matrix are scaled by `sim`.
- "convex" returns the doubly stochastic matrix from the last iteration of running the Frank-Wolfe algorithm with convex relaxation initialized at the barycenter. For this method, one needs to input two graphs `A` and `B`, as well as seeds if applicable.

Value

`init_start` returns a `nns`-by-`nns` doubly stochastic matrix as the start matrix in the graph matching iteration. If conduct a soft seeding graph matching, returns a `nns`-by-`nns` doubly stochastic matrix with 1's corresponding to the soft seeds and values at the other places are derived by different start method.

Examples

```
ss <- matrix(c(5, 4, 4, 3), nrow = 2)
# initialize start matrix without soft seeds
init_start(start = "bari", nns = 5)
init_start(start = "rds", nns = 3)
init_start(start = "rds_perm_bari", nns = 5)
init_start(start = "rds_from_sim", nns = 3, sim = matrix(runif(9), 3))

# initialize start matrix with soft seeds
init_start(start = "bari", nns = 5, ns = 1, soft_seeds = ss)
init_start(start = "rds", nns = 5, soft_seeds = ss)
init_start(start = "rds_perm_bari", nns = 5, soft_seeds = ss)

# initialize start matrix for convex graph matching
cgnp_pair <- sample_correlated_gnp_pair(n = 10, corr = 0.3, p = 0.5)
g1 <- cgnp_pair$graph1
g2 <- cgnp_pair$graph2
seeds <- 1:10 <= 2
init_start(start = "convex", nns = 8, A = g1, B = g2, seeds = seeds)

# FW graph matching with incorrect seeds to start at convex start
init_start(start = "convex", nns = 8, ns = 2, soft_seeds = ss, A = g1, B = g2, seeds = seeds)
```

largest_common_cc *Find the largest common connected subgraph (LCCS) of two graphs*

Description

Find the largest common connected subgraphs of two matched graphs, which is an induced connected subgraph of both graphs that has as many vertices as possible. The `largest_cc` function returns the largest connected subgraph of a single graph.

Usage

```
largest_common_cc(A, B, min_degree = 1)
```

```
largest_cc(A)
```

Arguments

A	A matrix or an igraph object. See check_graph . Must be single-layer.
B	A matrix or an igraph object. See check_graph . Must be single-layer.
min_degree	A number. Defines the level of connectedness of the obtained largest common connected subgraph. The induced subgraph is a graph with a minimum vertex-degree of at least min_degree.

Value

`largest_common_cc` returns the common largest connected subgraphs of two aligned graphs in the igraph object form and a logical vector indicating which vertices in the original graphs remain in the induced subgraph.

Examples

```
cgnp_pair <- sample_correlated_gnp_pair(n = 10, corr = 0.7, p = 0.2)
g1 <- cgnp_pair$graph1
g2 <- cgnp_pair$graph2
# put no constraint on the minimum degree of the common largest connect subgraph
lccs1 <- largest_common_cc(g1, g2, min_degree = 1)
# induced subgraph
lccs1$g1
lccs1$g2
# label of vertices of the induced subgraph in the original graph
igraph::V(g1)[lccs1$keep]

# obtain a common largest connect subgraph with each vertex having a minimum degree of 3
lccs3 <- largest_common_cc(g1, g2, min_degree = 3)

g <- igraph::sample_gnp(100, .01)
lcc <- largest_cc(g)
# induced subgraph
```



```
lcc$g
# label of vertices of the induced subgraph in the original graph
igraph::V(g)[lcc$keep]
```

pad

Pad a matrix object with extra rows/columns of 0s.

Description

Attempts are made to make this padding efficient by employing sparse graphs

Usage

```
pad(m, nr, nc = nr)
```

Arguments

m	matrix
nr	number of rows to add
nc	number of columns to add. (default = nr)

Value

m padded with nr rows and nc columns of zeros.

plot,igraph,igraph-method

Plotting methods for visualizing matches

Description

Two functions are provided, `match_plot_igraph` which makes a ball and stick plot from igraph objects and `match_plot_matrix` which shows an adjacency matrix plot.

Usage

```
## S4 method for signature 'igraph,igraph'
plot(x, y, match = NULL, color = TRUE, linetype = TRUE, ...)
```

```
## S4 method for signature 'Matrix,Matrix'
plot(x, y, match = NULL, col.regions = NULL, at = NULL, colorkey = NULL, ...)
```

Arguments

<code>x</code>	First graph, either an igraph object or a Matrix
<code>y</code>	second graph, either an igraph object or a Matrix
<code>match</code>	result from a match call. Requires element <code>corr</code> as a data.frame with names <code>corr_A</code> , <code>corr_B</code> .
<code>color</code>	Whether to color edges according to which graph(s) they are in.
<code>linetype</code>	Whether to set edge line types according to which graph(s) they are in.
<code>...</code>	additional parameters passed to either the igraph plot function or the Matrix image function.
<code>col.regions</code>	NULL for default colors, otherwise see image-methods
<code>at</code>	NULL for default at values for at (ensures zero is grey), otherwise see image-methods
<code>colorkey</code>	NULL for default colorkey, otherwise see image-methods

Details

Grey edges/pixels indicate common edges, blue indicates edges only in graph A and red represents edges only graph B. The corresponding linetypes are solid, long dash, and short dash.

The plots can be recreated from the output with the code

```
plot(g)
for g <- match_plot_igraph(...) and
col <- colorRampPalette(c("#AA4444", "#888888", "#44AA44"))
image(m, col.regions = col(256))
for m <- match_plot_match(...).
```

This only plots and returns the matched vertices.

Value

Both functions return values invisibly. `match_plot_igraph` returns the union of the matched graphs as an igraph object with additional edge attributes `edge_match`, `color`, `lty`. `match_plot_matrix` returns the difference between the matched graphs.

Examples

```
set.seed(123)
graphs <- sample_correlated_gnp_pair(20, .9, .3)
A <- graphs$graph1
B <- graphs$graph2
res <- gm(A, B, 1:4, method = "percolation")

plot(A, B, res)
plot(A[], B[], res)
```

 sample_correlated_gnp_pair

Sample correlated $G(n,p)$ random graphs

Description

Sample a pair of correlated $G(n,p)$ random graphs with correlation between two graphs being `corr` and edge probability being `p`.

Usage

```
sample_correlated_gnp_pair(n, corr, p, ncore = n, permutation = 1:n, ...)
```

Arguments

<code>n</code>	An integer. Number of total vertices for the sampled graphs.
<code>corr</code>	A number. The target Pearson correlation between the adjacency matrices of the generated graphs. It must be in $[0,1]$ interval.
<code>p</code>	A number. Edge probability between two vertices. It must be in open $[0,1]$ interval.
<code>ncore</code>	An integer. Number of core vertices.
<code>permutation</code>	A numeric vector to permute second graph.
<code>...</code>	Passed to <code>sample_gnp</code> .

Value

`sample_correlated_gnp_pair` returns a list of two igraph object, named `graph1` and `graph2`, whose adjacency matrix entries are correlated with `corr`. If sample two graphs with junk vertices, the first `ncore` vertices are core vertices and the rest are junk vertices.

References

V. Lyzinski and D. E. Fishkind and C. E. Priebe (2014), *Seeded Graph Matching for Correlated Erdos-Renyi Graphs*. J. Mach. Learn. Res., pages 3513-3540.

See Also

[sample_correlated_sbm_pair](#), [sample_correlated_rdp_g_pair](#)

Examples

```
sample_correlated_gnp_pair(n=50, corr=0.3, p=0.5, ncore=40)
sample_correlated_gnp_pair(n=5, corr=0.3, p=0.5, permutation=c(1,3,2,4,5))
```

sample_correlated_ieg_pair

Sample graphs from edge probability matrix and correlation matrix

Description

Sample a pair of graphs with specified edge probability and correlation between each pair of vertices.

Usage

```
sample_correlated_ieg_pair(
  n,
  p_mat,
  c_mat,
  ncore = n,
  directed = FALSE,
  loops = FALSE,
  permutation = 1:n
)

sample_correlated_rdpdg_pair(X, corr, ncore = nrow(X), ...)
```

Arguments

n	An integer. Number of total vertices for the sampled graphs.
p_mat	An n-by-n matrix. Edge probability matrix, each entry should be in the open (0,1) interval.
c_mat	An n-by-n matrix. The target Pearson correlation matrix, each entry should be in the open (0,1) interval.
ncore	An integer. Number of core vertices.
directed	Logical scalar, whether to generate directed graphs.
loops	Logical scalar, whether self-loops are allowed in the graph.
permutation	A numeric vector, permute second graph.
X	A matrix. Dot products matrix, each entry must be in open (0,1) interval.
corr	A number. The target Pearson correlation between the adjacency matrices of the generated graphs. It must be in open (0,1) interval.
...	Passed to sample_correlated_ieg_pair.

Value

sample_correlated_ieg_pair returns two igraph objects named graph1 and graph2. If sample two graphs with junk vertices, the first ncore vertices are core vertices and the rest are junk vertices.

sample_correlated_rdpdg_pair returns two igraph objects named graph1 and graph2 that are sampled from random dot product graphs model. If sample two graphs with junk vertices, the first ncore vertices are core vertices and the rest are junk vertices.

References

S. Young and E. Scheinerman (2007), *Random Dot Product Graph Models for Social Networks*. Proceedings of the 5th International Conference on Algorithms and Models for the Web-graph, pages 138-149.

F. Fang and D. Sussman and V. Lyzinski (2018), *Tractable Graph Matching via Soft Seeding*. <https://arxiv.org/abs/1807.09299>.

See Also

[sample_correlated_gnp_pair](#), [sample_correlated_sbm_pair](#)

Examples

```
n <- 50
p_mat <- matrix(runif(n^2),n)
c_mat <- matrix(runif(n^2),n)
sample_correlated_ieg_pair(n,p_mat,c_mat,ncore=40)

## sample a pair of igraph objects from random dot
## product graphs model with dimension 3 and scale 8
n <- 50
xdim <- 3
scale <- 8
X <- matrix(rgamma(n*(xdim+1),scale,1),n,xdim+1)
X <- X/rowSums(X)
X <- X[,1:xdim]
sample_correlated_rdp_g_pair(X,corr=0.5,ncore=40)
```

sample_correlated_sbm_pair

Sample graphs pair from stochastic block model

Description

Sample a pair of random graphs from stochastic block model with correlation between two graphs being corr and edge probability being p.

Usage

```
sample_correlated_sbm_pair(
  n,
  pref.matrix,
  block.sizes,
  corr,
  core.block.sizes = NULL,
  permutation = 1:n,
  ...
)
```

Arguments

n	An integer. Number of vertices in the graph.
pref.matrix	The matrix giving the Bernoulli rates. This is a K-by-K matrix, where k is the number of groups. The probability of creating an edge between vertices from groups i and j is given by element i, j. For undirected graphs, this matrix must be symmetric.
block.sizes	A numeric vector. Give the number of vertices in each group. The sum of the vector must match the number of vertices.
corr	A number. The target Pearson correlation between the adjacency matrices of the generated graphs. It must be in open (0,1) interval.
core.block.sizes	A numeric vector. Give the number of core vertices in each group. Entries should be smaller than block.sizes and the vector length should be the same as block.sizes.
permutation	A numeric vector, permute second graph.
...	Passed to sample_sbm.

Value

Returns a list of two igraph object, named graph1 and graph2. If sample two graphs with junk vertices, in each corresponding block the first core.block.sizes vertices are core vertices and the rest are junk vertices.

References

P. Holland and K. Laskey and S. Leinhardt (1983), *Stochastic Blockmodels: First Steps*. Social Networks, pages 109-137.

F. Fang and D. Sussman and V. Lyzinski (2018), *Tractable Graph Matching via Soft Seeding*. <https://arxiv.org/abs/1807.09299>.

See Also

[sample_correlated_gnp_pair](#), [sample_correlated_rdpdg_pair](#)

Examples

```
pm <- cbind( c(.1, .001), c(.001, .05) )
sample_correlated_sbm_pair(n=1000, pref.matrix=pm, block.sizes=c(300,700), corr=0.5)
sample_correlated_sbm_pair(n=1000, pref.matrix=pm, block.sizes=c(300,700), corr=0.5,
core.block.sizes=c(200,500))
```

split_igraph	<i>Split an igraph object into aligned graphs by attribute</i>
--------------	--

Description

Given an igraph object and an edge attribute, this function finds all unique values of the edge attribute in the graph and returns a list of igraph objects on the same vertex set where each element of the list has a graph containing only those edges with specified attributed.

Usage

```
split_igraph(g, e_attr, strip_vertex_attr = FALSE)
```

Arguments

g	An igraph object
e_attr	the name of an edge attribute in g
strip_vertex_attr	Whether to remove all vertex attribute from the new graphs

Value

A named list of igraph objects with names corresponding to the values of the edge attributes.

Examples

```
g <- igraph::sample_gnm(20, 60)
igraph::E(g)$color <-
  sample(c("red", "green"), 60, replace = TRUE)
split_igraph(g, "color")
```

splrMatrix-class	<i>Sparse Plus Low-Rank Matrices</i>
------------------	--------------------------------------

Description

An "S4" class for efficient computation with sparse plus low-rank matrices. Stores sparse plus low-rank matrices (e.g. from matrix factorization or centering graphs) of the form $x + a \%*\% t(b)$ for faster computation.

Usage

```
splr(x, a = NULL, b = NULL, rank = NULL, dimnames = list(NULL, NULL), ...)
```

```
## S4 method for signature 'Matrix,Matrix,Matrix'
```

```
splr(x, a = NULL, b = NULL, rank = NULL, dimnames = list(NULL, NULL), ...)
```

Arguments

x	as in "Matrix"
a	as in "Matrix"
b	as in "Matrix"
rank	rank of the matrix to be factorized.
dimnames	optional - the list of names for the matrix
...	as in "Matrix"

Value

splrMatrix object
splrMatrix object

Slots

x a sparse matrix
a a low-rank factor or a matrix
b optional. a low-rank factor for $a \%*\% t(b)$. if b is not provided, a will be factorized using [irlba](#) provided `factorize = TRUE`

See Also

Methods are documented in [splrMatrix_method](#). Other relevant methods are [splr_sparse_plus_constant](#) and

splr_sparse_plus_constant

Add a constant to a splrMatrix object

Description

Add a constant to a splrMatrix object

Usage

splr_sparse_plus_constant(x, a)

Arguments

x	sparse Matrix object
a	scalar

Value

new splrMatrix object $x + a$

summary,graphMatch-method

Summary methods for graphMatch objects

Description

Summary methods for graphMatch objects

Usage

```
## S4 method for signature 'graphMatch'  
summary(object, A = NULL, B = NULL, true_label = NULL, directed = NULL)
```

Arguments

object	graphMatch object
A	igraph or matrix-like object
B	igraph or matrix-like object
true_label	the true correspondence (if available)
directed	whether to treat the graphs as directed (TRUE) or not directed (FALSE) default is NULL which will treat the graphs as directed if either adjacency matrix is not symmetric.

Value

summary returns the graph matching formula, and a summary of graph matching results including the number of matches, the number of correct matches (if the true correspondence is available), and common edges, missing edges, extra edges, common non-edges and the objective function value.

Examples

```
set.seed(123)  
graphs <- sample_correlated_gnp_pair(20, .9, .3)  
A <- graphs$graph1  
B <- graphs$graph2  
match <- gm(A, B, 1:4, method = "percolation")  
  
summary(match, A, B)  
summary(match, A, B, true_label = 1:20) # also output the number of correct matches
```

Transportation	<i>Britain Transportation Network</i>
----------------	---------------------------------------

Description

The Britain Transportation Network reflects the transportation connections in the UK, with five layers representing ferry, rail, metro, coach, and bus.

Usage

```
data(Transportation)
```

Format

A list of length 3, corresponding to the template graph, world graph, and candidate data frame with first column indicating template node ID's and second column indicating world node ID's. The template graph and world graph are stored as lists of five adjacency matrices, representing ferry, rail, metro, coach, and bus transportation connections respectively.

Details

The data consists of a smaller template graph with 53 nodes and 56 connections across five layers, a larger world graph with candidates of the template graph with 2075 nodes and 8368 connections, and a list of candidate matches for each template node, where the true correspondence is guaranteed to be among the candidates.

The template graph was constructed based on a random walk starting from a randomly chosen hub node, a node that has connections in all the layers. All edges in the template are common edges shared by two graphs, where 40%, 24.1%, 37.5%, 31.7% and 25.6% of edges in the world graph are in template for each layer. All graphs are unweighted, directed, and do not have self-loops.

References

Gallotti, R., Barthelemy, M. (2015). *The multilayer temporal network of public transport in Great Britain*. Sci Data 2, 140056 . <https://doi.org/10.1038/sdata.2014.56>.

J. D. Moorman, Q. Chen, T. K. Tu, Z. M. Boyd and A. L. Bertozzi, (2018). *Filtering Methods for Subgraph Matching on Multiplex Networks*. 2018 IEEE International Conference on Big Data (Big Data), pp. 3980-3985, doi: 10.1109/BigData.2018.8622566.

See Also

The original Britain Transportation Network data is found here math.bu.edu/people/sussman/data/Transportation.rda. The template graph and world graph in the 'Transportation' data are induced subgraphs of the original graphs , keeping only the candidate nodes.

Examples

```
tm <- Transportation[[1]]
cm <- Transportation[[2]]
candidate <- Transportation[[3]]
tn <- nrow(tm[[1]])
wn <- nrow(cm[[1]])
similarity <- with(candidate, Matrix::sparseMatrix(i = tem, j = wor, x = 1,
                                                    dims = c(tn,wn)))
```

%%,graphMatch,ANY-method

Operator methods for graphMatch objects

Description

Methods to use [graphMatch](#) objects as operators on igraph and matrix-like objects.

Usage

```
## S4 method for signature 'graphMatch,ANY'
x %% y

## S4 method for signature 'ANY,graphMatch'
x %% y

## S4 method for signature 'graphMatch,Matrix'
x %% y

## S4 method for signature 'Matrix,graphMatch'
x %% y

## S4 method for signature 'graphMatch,igraph'
x %% y

## S4 method for signature 'igraph,graphMatch'
x %% y
```

Arguments

x	Either graphMatch object or a matrix-like object
y	Either graphMatch object or a matrix-like object

Value

These methods return an object of the same type as the non-graphMatch object. If m is the match of g1 to g2 (both igraph objects), then m permuted so as to match with g1. Conversely, g1 returns g1 permuted so as to match with g2.

Examples

```
set.seed(123)
cgnp_pair <- sample_correlated_gnp_pair(n = 10, corr = 0.3, p = 0.5)
g1 <- cgnp_pair$graph1
g2 <- cgnp_pair$graph2

# match g1 & g2 using FW methodology with indefinite relaxation
match <- gm(A = g1, B = g2, seeds = 1:3, method = 'indefinite')

# permute the second graph according to the match result: P %*% g2 %*% P^T
match %*% g2 # return an igraph object
# equivalent to the matrix operation
match[] %*% g2[] %*% t(match[])

match %*% g2[] # return a matrix
# equivalent to:
P <- match[]
P %*% g2[] %*% Matrix::t(P)

# the inverse operations are performed via right multiplication
all(g1[] %*% match == t(P) %*% g1[] %*% P)
```

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