# Package 'spatPomp'

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Type Package

Title Inference for Spatiotemporal Partially Observed Markov Processes

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URL https://github.com/kidusasfaw/spatPomp

**Description** Inference on panel data using spatiotemporal partially-observed Markov process (Spat-POMP) models. The 'spatPomp' package extends 'pomp' to include algorithms taking advantage of the spatial structure in order to assist with handling high dimensional processes. See Asfaw et al. (2024) <doi:10.48550/arXiv.2101.01157> for further description of the package.

**SystemRequirements** For Windows users, Rtools (see https://cran.r-project.org/bin/windows/Rtools/).

License GPL-3 Encoding UTF-8 LazyData true

BugReports https://github.com/kidusasfaw/spatPomp/issues/

**Depends** pomp (>= 5.4), R(>= 4.1), methods

LinkingTo pomp

Suggests doParallel (>= 1.0.11), parallel, doRNG

Imports foreach, dplyr, tidyr, stringr, abind, rlang, ggplot2

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# Description

The **spatPomp** package provides facilities for inference on panel data using spatiotemporal partially-observed Markov process (SPATPOMP) models. To do so, it relies on and extends a number of facilities that the **pomp** package provides for inference on time series data using partially-observed Markov process (POMP) models.

The **spatPomp** package concerns models consisting of a collection of interacting units. The methods in **spatPomp** may be applicable whether or not these units correspond to spatial locations.

# Data analysis using spatPomp

The first step in using **spatPomp** is to encode one's model(s) and data in objects of class spatPomp. This can be done via a call to the **spatPomp** constructor function.

# Extending the pomp platform for developing inference tools

**spatPomp** extends to panel data the general interface to the components of POMP models provided by **pomp**. In doing so, it contributes to the goal of the **pomp** project of facilitating the development of new algorithms in an environment where they can be tested and compared on a growing body of models and datasets.

#### **Documentation**

spatPomp is described by Asfaw et al. (2020)

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#### License

**spatPomp** is provided under the MIT License.

#### Author(s)

Kidus Asfaw, Joonha Park, Allister Ho, Edward Ionides, Aaron A. King

#### References

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

#### See Also

pomp

abf

Adapted Bagged Filter (ABF)

# **Description**

An algorithm for estimating the likelihood of a spatiotemporal partially-observed Markov process model. Running abf causes the algorithm to run bootstrap replicate jobs which each yield an imperfect adapted simulation. Simulating from the "adapted filter" distribution runs into a curse of dimensionality (COD) problem, which is mitigated by keeping particles in each replicate close to each other through resampling down to one particle per replicate at each observation time point. The adapted simulations are then weighted in a way that mitigates COD by making a weak coupling assumption to get an approximate filter distribution. As a by-product, we also get an estimate of the likelihood of the data.

# Usage

```
## S4 method for signature 'spatPomp'
abf(
  object,
  Nrep,
  Np,
  nbhd,
  params,
  tol = 1e-100,
    ...,
  verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'abfd_spatPomp'
abf(object, Nrep, Np, nbhd, tol, ..., verbose = getOption("verbose", FALSE))
```

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# Arguments

object	A spatPomp object.
Nrep	The number of bootstrap replicates for the adapted simulations.
Np	The number of particles used within each replicate for the adapted simulations.
nbhd	A neighborhood function with three arguments: object, time and unit. The function should return a list of two-element vectors that represent space-time neighbors of $(u,n)$ , which is represented by c(unit, time). See example below for more details.
params	Parameter vector, required if not available from the spatPomp model object.
tol	If the resampling weight for a particle is zero due to floating-point precision issues, it is set to the value of tol since resampling has to be done.
	Additional arguments can be used to replace model components.
verbose	logical; if TRUE, messages updating the user on progress will be printed to the

#### Value

Upon successful completion, abf() returns an object of class 'abfd\_spatPomp' containing the algorithmic parameters used to run abf() and the estimated likelihood.

### Methods

The following methods are available for such an object:

console.

logLik yields an estimate of the log-likelihood of the data under the model.

# Author(s)

Kidus Asfaw

#### References

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

### See Also

```
likelihood maximization algorithms: ienkf(), igirf, iubf, ibpf
Other likelihood evaluation algorithms: abfir(), bpfilter(), enkf(), girf()
```

# Examples

```
# Complete examples are provided in the package tests
## Not run:
# Create a simulation of a Brownian motion
b <- bm(U=2, N=5)
# Create a neighborhood function mapping a point in space-time</pre>
```

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```
# to a list of neighboring points in space-time
bm_nbhd <- function(object, time, unit) {
   nbhd_list = list()
   if(time > 1 && unit > 1){
      nbhd_list = c(nbhd_list, list(c(unit-1, time-1)))
   }
   return(nbhd_list)
}

# Run ABF specified number of Monte Carlo replicates and particles per replicate
abfd_bm <- abf(b, Nrep=2, Np=10, nbhd=bm_nbhd)

# Get the likelihood estimate from ABF
logLik(abfd_bm)

## End(Not run)</pre>
```

abfir

Adapted Bagged Filter with Intermediate Resampling (ABF-IR)

### **Description**

An algorithm for estimating the filter distribution and likelihood of a spatiotemporal partially-observed Markov process model. Running abfir causes the algorithm to run Monte Carlo replicated jobs which each carry out an adapted simulation using intermediate resampling. Adapted simulation is an easier task than filtering, since particles in each replicate remain close to each other. Intermediate resampling further assists against the curse of dimensionality (COD) problem for importance sampling. The adapted simulations are then weighted in a way that mitigates COD by making a weak coupling assumption to get an approximate filter distribution. As a by-product, we also get an approximation to the likelihood of the data.

### Usage

```
## S4 method for signature 'spatPomp'
abfir(
  object,
  Np,
  Nrep,
  nbhd,
  Ninter,
  tol = (1e-100),
  params,
  ...,
  verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'abfird_spatPomp'
abfir(object, Np, Nrep, nbhd, Ninter, tol, params, ...)
```

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#### **Arguments**

object A spatPomp object.

Np The number of particles used within each replicate for the adapted simulations.

Nrep The number of bootstrap replicates for the adapted simulations.

nbhd A neighborhood function with three arguments: object, time and unit. The

function should return a list of two-element vectors that represent space-time neighbors of (u, n), which is represented by c(unit, time). See example below

for more details.

Ninter the number of intermediate resampling time points. By default, this is set equal

to the number of units.

tol If the resampling weight for a particle is zero due to floating-point precision

issues, it is set to the value of tol since resampling has to be done.

params Parameter vector, required if not available from the spatPomp model object.

. . . Additional arguments can be used to replace model components.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

### Value

Upon successful completion, abfir() returns an object of class 'abfird\_spatPomp' containing the algorithmic parameters used to run abfir() and the estimated likelihood.

### Methods

The following methods are available for such an object:

logLik yields a biased estimate of the log-likelihood of the data under the model.

#### Author(s)

Kidus Asfaw

#### References

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

### See Also

likelihood maximization algorithms: ienkf(), igirf(), iubf(), ibpf()

Other likelihood evaluation algorithms: abf(), bpfilter(), enkf(), girf()

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### **Examples**

```
# Complete examples are provided in the package tests
## Not run:
# Create a simulation of a Brownian motion
b < -bm(U=2, N=5)
# Create a neighborhood function mapping a point in space-time
# to a list of ``neighboring points" in space-time
bm_nbhd <- function(object, time, unit) {</pre>
  nbhd_list = list()
  if(time > 1 \&\& unit > 1){
    nbhd_list = c(nbhd_list, list(c(unit-1, time-1)))
  return(nbhd_list)
}
# Run ABFIR with specified number of Monte Carlo replicates and particles
# per replicate
abfird_bm <- abfir(b,</pre>
                  Nrep = 2,
                  Np=10,
                  nbhd = bm_nbhd,
                  Ninter = length(unit_names(b)))
# Get the likelihood estimate from ABFIR
logLik(abfird_bm)
## End(Not run)
```

arma\_benchmark

Calculated log-ARMA log-likelihood benchmark for spatPomp models

### Description

Fits independent log-ARMA models for each unit, and calculates the conditional log-likelihood for each observation, as well as log-likelihood for each unit and total log-likelihood. A simple tool, but one with practical applicability, as demonstrated by King et al (2008) and Wheeler et al (2023). This function is designed for non-negative data, and adds 1 to each observation to avoid log(0).

# Usage

```
arma_benchmark(spo, order = c(2, 0, 1))
```

#### **Arguments**

spo A spatPomp object

order A triple (p,d,q) for the ARIMA model fitted to the data. It is intended that d=0

### Author(s)

Edward L. Ionides

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### References

King, A. A., Ionides, E. L., Pascual, M. and Bouma, M. J. (2008). Inapparent infections and cholera dynamics. Nature 454 877-880.

Wheeler, J., Rosengart, A. L., Jiang, Z., Tan, K., Treutle, N. and Ionides, E. L. (2023). Informing policy via dynamic models: Cholera in Haiti. arxiv:2301.08979.

### See Also

```
Other utilities: expand_params()
```

### **Examples**

```
# Complete examples are provided in the package tests
## Not run:
m <- he10(U = 5)
arma_benchmark(m)
## End(Not run)</pre>
```

as.data.frame

Coerce to data frame

### **Description**

**spatPomp** objects can be recast as data frames.

### Usage

```
## S3 method for class 'spatPomp'
as.data.frame(x, ...)
```

### **Arguments**

x a spatPomp object.

additional arguments to be passed to or from methods.

#### **Details**

When object is a simple 'spatPomp' object, as(object, "data.frame") or as.data.frame(object) results in a data frame with the times, units, observables, states (if known), and interpolated covariates (if any).

# Value

A 'data.frame' with columns for time, spatial unit and observations.

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bm

Brownian motion spatPomp simulator

### Description

Generate a class 'spatPomp' object representing a U-dimensional Brownian motion with spatial correlation decaying geometrically with distance around a circle. The model is defined in continuous time though in this case an Euler approximation is exact at the evaluation times.

### Usage

```
bm(U = 5, N = 100, delta_t = 0.1)
```

### **Arguments**

U A length-one numeric signifying dimension of the process.

N A length-one numeric signifying the number of observation time steps to evolve

the process.

delta\_t Process simulations are performed every delta\_t time units whereas observa-

tions occur every one time unit

#### Value

An object of class 'spatPomp' representing a simulation from a U-dimensional Brownian motion

### Author(s)

Edward L. Ionides

# See Also

```
Other spatPomp model generators: bm2(), gbm(), he10(), lorenz(), measles()
```

# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
b <- bm(U=4, N=20)
# See all the model specifications of the object
spy(b)
# Examples of methodologies applied to this model
# are provided in the tests directory
## End(Not run)</pre>
```

bm2

bm2	Brownian motion spatPomp generator with shared or unit-specific pa-
	rameters

# Description

An extension of bm allowing for shared or unit-specific parameters. Generate a class 'spatPomp' object representing a U-dimensional Brownian motion with spatial correlation decaying geometrically with distance around a circle. The model is defined in continuous time though in this case an Euler approximation is exact at the evaluation times.

# Usage

```
bm2(
    U = 5,
    N = 100,
    delta_t = 0.1,
    unit_specific_names = "rho",
    shared_names = NULL,
    unit_params = c(rho = 0.4, sigma = 1, tau = 1, X_0 = 0)
)
```

### **Arguments**

U	A length-one numeric signifying dimension of the process.					
N	A length-one numeric signifying the number of observation time steps to evolve the process.					
delta_t	Process simulations are performed every delta_t time units whereas observations occur every one time unit					
unit_specific_names						
	determines which parameters take a different value for each unit. Cannot be specified if shared_names is specified. each unit. Other parameters are considered shared between all units.					
shared_names	identifies parameters that have common shared value for all units, which by default is all parameters.					
unit_params	parameter values used to build the object, copied across each unit for unit-specific parameters					

# Value

An object of class 'spatPomp' representing a simulation from a U-dimensional Brownian motion

# Author(s)

Edward L. Ionides

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### See Also

```
Other spatPomp model generators: bm(), gbm(), he10(), lorenz(), measles()
```

#### **Examples**

```
# Complete examples are provided in the package tests
## Not run:
b <- bm2(U=4, N=20, shared_names="rho", unit_specific_names=c("sigma", "tau"))
# See all the model specifications of the object
spy(b)
# Examples of methodologies applied to this model
# are provided in the tests directory
## End(Not run)</pre>
```

bm2\_kalman\_logLik

Exact log-likelihood for Brownian motion spatPomp generator with shared or unit-specific parameters

# Description

Computes the exact likelihood for a model constructed using bm2, using the Kalman filter. This model is useful for testing methods for models with unit-specific parameters, or method such as ibpf which require a unit-specific extension of shared parameters.

### Usage

```
bm2_kalman_logLik(bm2_object, params = coef(bm2_object))
```

# Arguments

bm2\_object A spatPomp model built using bm2.

params A parameter vector at which to evaluate the log-likelihood. whereas observa-

tions occur every one time unit

#### Value

A numeric value for the log-likelihood.

### Author(s)

Edward L. Ionides

bm\_kalman\_logLik

### **Examples**

```
# Further examples are provided in the tests directory
## Not run:
b <- bm2()
bm2_kalman_logLik(b)
## End(Not run)</pre>
```

bm\_kalman\_logLik

Exact log-likelihood for Brownian motion spatPomp generator

# Description

Computes the exact likelihood for a model constructed using bm, using the Kalman filter. This model is useful for testing methods in a situation where an exact answer is available

# Usage

```
bm_kalman_logLik(bm_object, params = coef(bm_object))
```

### Arguments

bm\_object A spatPomp model built using bm.

params A parameter vector at which to evaluate the log-likelihood. whereas observa-

tions occur every one time unit

### Value

A numeric value for the log-likelihood.

# Author(s)

Edward L. Ionides

### **Examples**

```
# Further examples are provided in the tests directory
## Not run:
b <- bm()
bm_kalman_logLik(b)
## End(Not run)</pre>
```

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bpfilter

Block particle filter (BPF)

### Description

An implementation of the block particle filter algorithm of Rebeschini and van Handel (2015), which is used to estimate the filter distribution of a spatiotemporal partially-observed Markov process. bpfilter requires a partition of the spatial units which can be provided by either the block\_size or the block\_list argument. The elements of the partition are called blocks. We perform resampling for each block independently based on sample weights within the block. Each resampled block only contains latent states for the spatial components within the block which allows for a "cross-pollination" of particles where the highest weighted segments of each particle are more likely to be resampled and get combined with resampled components of other particles. The method mitigates the curse of dimensionality by resampling locally.

# Usage

```
## S4 method for signature 'missing'
bpfilter(object, ...)
## S4 method for signature 'ANY'
bpfilter(object, ...)
## S4 method for signature 'spatPomp'
bpfilter(
  object,
 Nρ,
  block_size,
  block_list,
  save_states,
  filter_traj,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'bpfilterd_spatPomp'
bpfilter(
  object,
  Np,
  block_size,
  block_list,
  save_states,
  filter_traj,
  verbose = getOption("verbose", FALSE)
)
```

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### **Arguments**

object	A spatPomp object.
	If a params argument is specified, bpfilter will estimate the likelihood at that parameter set instead of at coef(object).
Np	The number of particles used within each replicate for the adapted simulations.
block_size	The number of spatial units per block. If this is provided, the method subdivides units approximately evenly into blocks with size block_size.
block_list	List that specifies an exact partition of the spatial units. Each partition element, or block, is an integer vector of neighboring units.
save_states	logical. If True, the state-vector for each particle and block is saved.
filter_traj	logical; if TRUE, a filtered trajectory is returned for the state variables and parameters.
verbose	logical; if TRUE, messages updating the user on progress will be printed to the console.

### Value

Upon successful completion, bpfilter() returns an object of class 'bpfilterd\_spatPomp' containing the algorithmic parameters used to run bpfilter() and the estimated likelihood.

#### **Details**

Only one of block\_size or block\_list should be specified. If both or neither is provided, an error is triggered.

# Methods

The following methods are available for such an object:

logLik yields an estimate of the log-likelihood of the data under the model.

# Author(s)

Kidus Asfaw

# References

Rebeschini, P., & Van Handel, R. (2015). Can local particle filters beat the curse of dimensionality?. *The Annals of Applied Probability*, **25**(5), 2809-2866.

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

### See Also

```
likelihood maximization algorithms: ienkf(), igirf(), iubf(), ibpf()
Other likelihood evaluation algorithms: abf(), abfir(), enkf(), girf()
```

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### **Examples**

city\_data\_UK

City data in the United Kingdom

# **Description**

Population and birth information about cities in England and Wales during the measles pre-vaccine era.

# **Details**

Data includes births and population at bi-weekly observations from 40 cities and towns.

### Value

a 'data.frame' of the 40 largest cities and towns in the UK and Wales, their latitude, longitude and mean population during the measles pre-vaccine period.

#### References

Dalziel, Benjamin D. et al. (2016) Persistent chaos of measles epidemics in the prevaccination United States caused by a small change in seasonal transmission patterns. *PLoS Computational Biology*, **12(2)**, e1004655. doi:10.5061/dryad.r4q34

### See Also

Other datasets: measlesUK

concat 17

concat Concatenate

# **Description**

Concatenate two or more 'pomp' objects into a list-like 'listie'.

# Usage

```
## S3 method for class 'SpatPomp' c(...)
```

# Arguments

... elements to be recursively combined into a 'listie'

### **Details**

concat applied to one or more 'pomp' objects or lists of 'pomp' objects converts the list into a 'listie'. In particular, concat(A,B,C) is equivalent to do.call(c,unlist(list(A,B,C))).

dunit\_measure

dunit\_measure dunit\_measure evaluates the unit measurement density of a unit's observation given the entire state

# Description

dunit\_measure dunit\_measure evaluates the unit measurement density of a unit's observation given the entire state

# Usage

```
## S4 method for signature 'spatPomp'
dunit_measure(object, y, x, unit, time, params, log = TRUE, ...)
```

### **Arguments**

object	An object of class spatPomp
у	A U by 1 matrix of observations for all units
X	A state vector for all units
unit	The unit for which to evaluate the unit measurement density
time	The time for which to evaluate the unit measurement density
params	parameters at which to evaluate the unit measurement density
log	logical; should the density be returned on log scale?
	additional arguments will be ignored

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#### Value

A class 'matrix' with the unit measurement density for spatial unit unit corresponding to the corresponding measurement in y and states in x.

### **Examples**

```
# Complete examples are provided in the package tests
## Not run:
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
dunit_measure(b, y=o, x=s, unit=1, time=1, params=p)
## End(Not run)</pre>
```

enkf

Generalized Ensemble Kalman filter (EnKF)

### **Description**

A function to perform filtering using the ensemble Kalman filter of Evensen, G. (1994). This function is generalized to allow for an measurement covariance matrix that varies over time. This is useful if the measurement model varies with the state.

#### Usage

```
## S4 method for signature 'spatPomp'
enkf(data, Np, ..., verbose = getOption("verbose", FALSE))
```

### **Arguments**

data A spatPomp object.

Np The number of Monte Carlo particles used to approximate the filter distribution.

... Additional arguments can be used to replace model components.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

#### Value

An object of class 'enkfd\_spatPomp' that contains the estimate of the log likelihood (via the loglik attribute), algorithmic parameters used to run enkf(). Also included are estimated filter means, prediction means and forecasts that are generated during an enkf() run.

eunit\_measure 19

### References

G. Evensen. Sequential data assimilation with a nonlinear quasi-geostrophic model using Monte Carlo methods to forecast error statistics. *Journal of Geophysical Research: Oceans* **99**, 10143–10162, 1994.

- G. Evensen. Data assimilation: the ensemble Kalman filter. Springer-Verlag, 2009.
- J.L. Anderson. An Ensemble Adjustment Kalman Filter for Data Assimilation. *Monthly Weather Review* **129**, 2884–2903, 2001.

### See Also

```
ienkf(), igirf, iubf, ibpf
Other likelihood evaluation algorithms: abf(), abfir(), bpfilter(), girf()
```

# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
# Create a simulation of a Brownian motion
b <- bm(U=2, N=5)

# Run EnKF
enkfd_bm <- enkf(b, Np = 20)

# Get a likelihood estimate
logLik(enkfd_bm)

## End(Not run)</pre>
```

eunit\_measure

eunit\_measure

### **Description**

eunit\_measure evaluates the expectation of a unit's observation given the entire state

# Usage

```
## S4 method for signature 'spatPomp'
eunit_measure(object, x, unit, time, params, Np = 1, log = FALSE)
```

# **Arguments**

object	An object of class spatPomp
x	A state vector for all units
unit	The unit for which to evaluate the expectation
time	The time for which to evaluate the expectation

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params	parameters at which to evaluate the unit expectation
Np	numeric; defaults to 1 and the user need not change this
log	logical; should the density be returned on log scale?

#### Value

A class 'matrix' with the unit expected observation for spatial unit unit corresponding to the corresponding states in x.

# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
eunit_measure(b, x=s, unit=2, time=1, params=p)
## End(Not run)</pre>
```

expand\_params

Book-keeping functions for working with expanded parameters

### **Description**

Iterated block particle filters require shared parameters to be expanded into having a value at each unit. expand\_params, contract\_params and mean\_by\_unit provide tools for moving between representations. For a unit-specific expansion of a shared parameter, all the values for different units should be the same, and mean\_by\_unit ensures this by taking an average.

# Usage

```
expand_params(params, expandedParNames, U)
contract_params(params, expandedParNames, U, average = FALSE)
mean_by_unit(params, expandedParNames, U)
```

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### Arguments

params Input parameter vector

expandedParNames

character vector of parameters that are, or should be, expanded. These names

should have no numerical suffix 1:U.

U Number of units

average Logical value for whether contract\_params should average unequal values

#### **Details**

These functions assume that expanded parameters have names ending in "1" through "U", where U is the number of units. Contracted parameters, meaning any parameter that is not expanded, should have a name ending in "1". This numerical suffix convention is useful for writing model-building code that allows parameters to be either expanded or contracted.

### See Also

Other utilities: arma\_benchmark()

gbm

Geometric Brownian motion spatPomp simulator

# **Description**

Generate a spatPomp object representing a U-dimensional geometric Brownian motion with spatial correlation decaying geometrically with distance around a circle. The model is defined in continuous time, but an Euler approximation is used for this numerical implementation.

### Usage

```
gbm(U = 5, N = 100, delta_t = 0.1, IVP_values = 1, delta_obs = 1)
```

# **Arguments**

U A length-one numeric signifying dimension of the process.

N A length-one numeric signifying the number of time steps to evolve the process.

delta\_t process simulations are performed every delta\_t time units

IVP\_values initial value parameters for the latent states
delta\_obs observations occur every delta\_obs time units

#### Value

An object of class 'spatPomp' representing a simulation from a U-dimensional geometric Brownian motion

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### Author(s)

Kidus Asfaw

#### References

Asfaw, K. T. (2021). Simulation-based Inference for Partially Observed Markov Process Models with Spatial Coupling. University of Michigan Doctoral dissertation. doi:10.7302/2751

### See Also

```
Other spatPomp model generators: bm(), bm2(), he10(), lorenz(), measles()
```

# **Examples**

```
# Complete examples are provided in the package tests ## Not run: g \leftarrow gbm(U=4, N=20) # See all the model specifications of the object spy(g) ## End(Not run)
```

girf

Guided intermediate resampling filter (GIRF)

# **Description**

An implementation of the algorithm of Park and Ionides (2020), following the pseudocode in Asfaw et al. (2020).

### Usage

```
## S4 method for signature 'missing'
girf(object, ...)

## S4 method for signature 'ANY'
girf(object, ...)

## S4 method for signature 'spatPomp'
girf(
   object,
   Np,
   Ninter,
   lookahead = 1,
   Nguide,
   kind = c("bootstrap", "moment"),
   tol,
```

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```
verbose = getOption("verbose", FALSE)
)

## S4 method for signature 'girfd_spatPomp'
girf(
  object,
  Np,
  Ninter,
  lookahead,
  Nguide,
  kind = c("bootstrap", "moment"),
  tol,
  ...
)
```

#### Arguments

object A spatPomp object.
... Additional arguments can be used to replace model components.

Np The number of particles used within each replicate for the adapted simulations.

Ninter the number of intermediate resampling time points. By default, this is set equal

to the number of units.

lookahead The number of future observations included in the guide function.

Nguide The number of simulations used to estimate state process uncertainty for each

particle.

kind One of two types of guide function construction. Defaults to 'bootstrap'. See

Park and Ionides (2020) for more details.

tol If all of the guide function evaluations become too small (beyond floating-point

precision limits), we set them to this value.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

### Value

Upon successful completion, girf() returns an object of class 'girfd\_spatPomp' which contains the algorithmic parameters that were used to run girf() and the resulting log likelihood estimate.

#### Methods

The following methods are available for such an object:

logLik yields an unbiased estimate of the log-likelihood of the data under the model.

### Author(s)

Kidus Asfaw

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#### References

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, doi:10.1007/s11222020099573

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

#### See Also

```
likelihood maximization algorithms: ienkf(), igirf(), iubf(), ibpf()
Other likelihood evaluation algorithms: abf(), abfir(), bpfilter(), enkf()
```

# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
# Create a simulation of a Brownian motion
b < -bm(U=2, N=5)
# Run GIRF
girfd_bm <- girf(b,
                 Np = 10,
                 Ninter = length(unit_names(b)),
                 lookahead = 1,
                 Nguide = 10
# Get the likelihood estimate from GIRF
logLik(girfd_bm)
# Compare with the likelihood estimate from particle filter
pfd_bm <- pfilter(b, Np = 10)</pre>
logLik(pfd_bm)
## End(Not run)
```

he10

Measles in UK: spatPomp generator with shared or unit-specific parameters

# **Description**

Generate a spatPomp object for measles adding spatial coupling to The model and data from He et al. (2010) with gravity transport as in Park and Ionides (2020). Other transport models may be added in future. The data in the object matches He et al. (2010). The model matches that analysis in the specific case where there is no coupling and all parameters are unit-specific.

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### Usage

```
he10(
    U = 6,
    dt = 2/365,
    Tmax = 1964,
    expandedParNames = c("alpha", "iota", "R0", "cohort", "amplitude", "gamma", "sigma",
        "sigmaSE", "rho", "psi", "g", "S_0", "E_0", "I_0"),
    basic_params = c(alpha = 1, iota = 0, R0 = 30, cohort = 0, amplitude = 0.5, gamma = 52,
        sigma = 52, mu = 0.02, sigmaSE = 0.15, rho = 0.5, psi = 0.15, g = 400, S_0 = 0.032,
        E_0 = 5e-05, I_0 = 4e-05),
    towns_selected = NULL
)
```

#### **Arguments**

U A length-one numeric signifying the number of cities to be represented in the

spatPomp object. Default U=20 gives all the towns studied by He et al., the 10

largest and 10 selected smaller towns.

dt a numeric (in unit of years) that is used as the Euler time-increment for simulat-

ing measles data.

Tmax Upper time for the window used to construct the object. The lower time is fixed

at 1950.0. The default value matches He et al (2010).

expandedParNames

specifies the names of parameters which take unit-specific values. Remaining

parameters take a single, shared value for all units.

basic\_params A candidate parameter vector in the basic format, i.e., no unit-specific parame-

ters or unit-related name extensions.

towns\_selected A numeric vector of towns to be modeled. Defaults to 1:U, with cities ranked

by decreasing population and 1 being London.

#### **Details**

The code for this spatPomp has duplication with measles(), but in future the two models may diverge. The measles() spatPomp is a simplified situation useful for testing some methods. However, measles() does not permit unit-specific parameters, which he10() allows. Also, the structure of this spatPomp is compatible with the spatiotemporal iterated filtering algorithm ibpf(). This requires shared parameters to be represented with a value for each unit, which should be the same for each unit in a valid model instance but may vary between units while optimizing.

### Value

An object of class 'spatPomp' representing a U-dimensional spatially coupled measles POMP model.

#### Relationship to published analysis

The model generator he10() differs from measles() in some details necessitated to reproduce the results of He et al (2010). The measles() model follows the decision of Park and Ionides (2020)

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and Ionides et al (2021) to apply the mixing exponent  $\alpha_u$  to  $(I_u/P_u)$  rather than just to  $I_u$ . he10() does this for the infections arising from individuals traveling to another town (which don't arise for the panel model of He et al (2010)). However, for infections arising within a city, in order to reproduce the results of He et al (2010), he10() uses  $(I_u^{\alpha_u}/P_u)$ . This is not fully documented in the text of Ionides et al (2022). Models fitted to data have  $alpha_u$  close to 1, so this issue may be negligible in practice.

Another discrepancy between the he10() code and the mathematical model written by Ionides et al (2022) arises in whether individuals traveling from u to v use mixing exponent  $\alpha_u$  or  $\alpha_v$ . Ionides et al (2022) wrote u but the code used implemented v. The implementation in he10() matches the implementation of Ionides et al (2022) and so uses v.

It might seem surprising that immigrant infections affect only the first term in the expression for  $\mu_{SE}$  in Ionides et al (2022), and in the corresponding he10() code. This immigration term is needed in the first term to make the model of He et al (2010) a proper sub-model, when coupling is removed by setting the gravitational constant parameter equal to zero. When this constant is allowed to be positive, the role of immigrant infections transmitting to traveling individuals is anticipated to be a negligible, second-order effect which has been omitted from the model.

#### Note

This function goes through a typical workflow of constructing a typical spatPomp object (1-4 below). This allows the user to have a file that replicates the exercise of model building as well as function that creates a typical nonlinear model in epidemiology in case they want to test a new inference methodology. We purposely do not modularize this function because it is not an operational piece of the package and is instead useful as an example.

- 1. Getting a measurements data.frame with columns for times, spatial units and measurements.
- 2. Getting a covariates data.frame with columns for times, spatial units and covariate data.
- 3. Constructing model components (latent state initializer, latent state transition simulator and measurement model). Depending on the methods used, the user may have to supply a vectorfield to be integrated that represents the deterministic skeleton of the latent process.
- 4. Bringing all the data and model components together to form a spatPomp object via a call to spatPomp().

### Author(s)

Edward L. Ionides

### References

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

He, D., Ionides, E. L., and King, A. A. (2010). Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface*, 7(43), 271-283. doi:10.1098/rsif.2009.0151

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

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Ionides, E. L., Ning, N., and Wheeler, J. (2022). An iterated block particle filter for inference on coupled dynamic systems with shared and unit-specific parameters. *Statistica Sinica*, to appear. doi:10.48550/arXiv.2206.03837

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, doi:10.1007/s11222020099573

#### See Also

```
he10coordinates, he10measles, he10mle, he10demography

Other spatPomp model generators: bm(), bm2(), gbm(), lorenz(), measles()
```

# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
m <- he10(U = 5)
# See all the model specifications of the object
spy(m)
## End(Not run)</pre>
```

he10coordinates

City data in the United Kingdom

# Description

Longitude and lattitude for the 20 towns in England and Wales studied by He et al (2010).

### Value

a 'data.frame' of longitude and lattitude for each town.

### References

He, D., Ionides, E. L., and King, A. A. (2010). Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface*, 7(43), 271-283. doi:10.1098/rsif.2009.0151

### See Also

Other datasets he10: he10demography, he10measles, he10mle

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he10demography

Demographic data for 20 towns in the United Kingdom

### **Description**

Population and birth information for some towns in England and Wales during the measles prevaccine era.

#### **Details**

Data are annual statistics for the 20 towns analyzed by He et al (2010).

#### Value

a 'data.frame' of with variables town, year, pop and births.

#### References

He, D., Ionides, E. L., and King, A. A. (2010). Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface*, 7(43), 271-283. doi:10.1098/rsif.2009.0151

### See Also

Other datasets he10: he10coordinates, he10measles, he10mle

he10measles

Measles in the United Kingdom

#### **Description**

Measles case data from various cities and towns in England and Wales during the pre-vaccine era.

### **Details**

Data are weekly case counts for the 20 towns analyzed by He et al (2010).

#### Value

a 'data.frame' of reported measles cases for 20 towns, analyzed by He et al (2010).

### References

He, D., Ionides, E. L., and King, A. A. (2010). Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface*, 7(43), 271-283. doi:10.1098/rsif.2009.0151

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### See Also

Other datasets he10: he10coordinates, he10demography, he10mle

he10mle

Measles in the United Kingdom: MLE from He et al (2010)

# **Description**

Maximum likelihood estimate for fitting a susceptible-exposed-infected- recovered model to the measles case report data analyzed by He et al (2010). The values are similar, but not identical, to those reported by He et al.

### Value

a 'data.frame' containing the estimated parameters.

#### References

He, D., Ionides, E. L., and King, A. A. (2010). Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface*, 7(43), 271-283. doi:10.1098/rsif.2009.0151

# See Also

Other datasets he10: he10coordinates, he10demography, he10measles

ibpf

Iterated block particle filter (IBPF)

# Description

An iterated block particle filter, for both shared and unit-specific parameters. We require that the spatPomp has been constructed to have a unit-specific parameter "thetau" for unit u corresponding to an estimated parameter "theta", whether theta is shared or unit-specific. This permits IBPF to implement a spatiotemporal random walk to estimate theta. We require that rw.sd is positive for, and only for, all parameters of the form "thetau" if "theta" is listed in sharedParNames or unitParNames.

ibpf

# Usage

```
## S4 method for signature 'missing'
ibpf(data, ...)
## S4 method for signature 'ANY'
ibpf(data, ...)
## S4 method for signature 'spatPomp'
ibpf(
 data,
 Nbpf,
 Nρ,
 rw.sd,
 sharedParNames,
 unitParNames,
  cooling.type = "geometric",
  cooling.fraction.50,
 block_size,
 block_list,
 spat_regression,
 verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'ibpfd_spatPomp'
ibpf(
 data,
 Nbpf,
 Nρ,
 rw.sd,
  sharedParNames,
 unitParNames,
 cooling.type = "geometric",
  cooling.fraction.50,
 block_size,
 block_list,
 spat_regression,
 verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'bpfilterd_spatPomp'
ibpf(
 data,
 Nbpf,
 Nρ,
  rw.sd,
  sharedParNames,
```

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```
unitParNames,
  cooling.type = "geometric",
  cooling.fraction.50,
  block_size,
  block_list,
  spat_regression,
  verbose = getOption("verbose", FALSE)
)
```

#### **Arguments**

data

either a data frame holding the time series data, or an object of class 'pomp', i.e., the output of another **pomp** calculation. Internally, data will be coerced to an array with storage-mode double.

If a params argument is specified, bpfilter will estimate the likelihood at that parameter set instead of at coef(object).

Nbpf

the number of iterations of perturbed BPF.

Np

The number of particles used within each replicate for the adapted simulations.

rw.sd

specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw\_sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

```
ifelse(time==time[1],s,0).
```

Likewise, ivp(s, lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

sharedParNames estimated parameters that are equal for each unit.

unitParNames

estimated parameters that are different for each unit.

cooling.type, cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

block size

The number of spatial units per block. If this is provided, the method subdivides units approximately evenly into blocks with size block\_size.

block\_list

List that specifies an exact partition of the spatial units. Each partition element, or block, is an integer vector of neighboring units.

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```
spat_regression
```

fraction of each extended parameter regressed toward the unit mean. Not re-

quired when all parameters are unit-specific.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

#### Value

Upon successful completion, ibpf returns an object of class 'ibpfd\_spatPomp'.

#### Methods

The following methods are available for such an object:

coef gives the Monte Carlo estimate of the maximum likelihood.

#### Author(s)

Edward L. Ionides

#### References

Ionides, E. L., Ning, N., and Wheeler, J. (2022). An iterated block particle filter for inference on coupled dynamic systems with shared and unit-specific parameters. *Statistica Sinica*, to appear. doi:10.48550/arXiv.2206.03837

# See Also

```
likelihood evaluation algorithms: girf(), enkf(), bpfilter(), abf(), abfir()
Other likelihood maximization algorithms: ienkf(), igirf(), iubf()
```

# **Examples**

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```
block_size=2
)

# Get a likelihood estimate
logLik(b2_ibpf)

## End(Not run)
```

ienkf

Iterated ensemble Kalman filter (IEnKF)

# **Description**

An implementation of a parameter estimation algorithm that uses the ensemble Kalman filter (Evensen, G. (1994)) to perform the filtering step in the parameter-perturbed iterated filtering scheme of Ionides et al. (2015) following the pseudocode in Asfaw, et al. (2020).

### Usage

```
## S4 method for signature 'spatPomp'
ienkf(
  data,
  Nenkf = 1,
  rw.sd,
  cooling.type = c("geometric", "hyperbolic"),
  cooling.fraction.50,
  Np,
  ...,
  verbose = getOption("verbose", FALSE)
)
```

# **Arguments**

data an object of class spatPomp

Nenkf number of iterations of perturbed EnKF.

rw.sd

specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw\_sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

```
ifelse(time==time[1],s,0).
Likewise, ivp(s,lag) is equivalent to
ifelse(time==time[lag],s,0).
```

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See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type, cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below (under "Specifying the perturbations") for more detail.

Np The number of particles used within each replicate for the adapted simulations.

... Additional arguments can be used to replace model components.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

#### Value

Upon successful completion, ienkf returns an object of class 'ienkfd\_spatPomp'. This object contains the convergence record of the iterative algorithm with respect to the likelihood and the parameters of the model (which can be accessed using the traces attribute) as well as a final parameter estimate, which can be accessed using the coef().

#### Methods

The following methods are available for such an object:

coef gives the Monte Carlo estimate of the maximum likelihood.

# Author(s)

Kidus Asfaw

#### References

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

Evensen, G. (1994) Sequential data assimilation with a nonlinear quasi-geostrophic model using Monte Carlo methods to forecast error statistics Journal of Geophysical Research: Oceans 99:10143–10162

Evensen, G. (2009) Data assimilation: the ensemble Kalman filter Springer-Verlag.

Anderson, J. L. (2001) An Ensemble Adjustment Kalman Filter for Data Assimilation Monthly Weather Review 129:2884–2903

#### See Also

likelihood evaluation algorithms: girf(), enkf(), bpfilter(), abf(), abfir()
Other likelihood maximization algorithms: ibpf(), igirf(), iubf()

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igirf

Iterated guided intermediate resampling filter (IGIRF)

### **Description**

An implementation of a parameter estimation algorithm combining the intermediate resampling scheme of the guided intermediate resampling filter of Park and Ionides (2020) and the parameter perturbation scheme of Ionides et al. (2015) following the pseudocode in Asfaw, et al. (2020).

# Usage

```
## S4 method for signature 'missing'
igirf(data, ...)
## S4 method for signature 'ANY'
igirf(data, ...)
## S4 method for signature 'spatPomp'
igirf(
  data,
 Ngirf,
 Nρ,
  rw.sd,
  cooling.type,
  cooling.fraction.50,
 Ninter,
  lookahead = 1,
 Nguide,
  kind = c("bootstrap", "moment"),
  tol = 1e-100,
  verbose = getOption("verbose", FALSE)
)
## S4 method for signature 'igirfd_spatPomp'
igirf(
 data,
 Ngirf,
 Nρ,
  rw.sd,
  cooling.type,
  cooling.fraction.50,
 Ninter,
  lookahead,
 Nguide,
  kind = c("bootstrap", "moment"),
  tol,
```

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```
...,
verbose = getOption("verbose", FALSE)
)
```

#### **Arguments**

data an object of class spatPomp or igirfd\_spatPomp

... Additional arguments can be used to replace model components.

Ngirf the number of iterations of parameter-perturbed GIRF.

Np The number of particles used within each replicate for the adapted simulations.

rw.sd specification of the magnitude of the random-walk perturbations that will be

applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw\_sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

ifelse(time==time[1],s,0).

Likewise, ivp(s,lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type, cooling.fraction.50

Ninter

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below

(under "Specifying the perturbations") for more detail.

the number of intermediate resampling time points. By default, this is set equal

to the number of units.

lookahead The number of future observations included in the guide function.

Nguide The number of simulations used to estimate state process uncertainty for each

particle.

kind One of two types of guide function construction. Defaults to 'bootstrap'. See

Park and Ionides (2020) for more details.

tol If all of the guide function evaluations become too small (beyond floating-point

precision limits), we set them to this value.

verbose logical; if TRUE, messages updating the user on progress will be printed to the

console.

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#### Value

Upon successful completion, <code>igirf()</code> returns an object of class 'igirfd\_spatPomp'. This object contains the convergence record of the iterative algorithm with respect to the likelihood and the parameters of the model (which can be accessed using the traces attribute) as well as a final parameter estimate, which can be accessed using the <code>coef()</code>. The algorithmic parameters used to run <code>igirf()</code> are also included.

#### Methods

The following methods are available for such an object:

coef gives the Monte Carlo maximum likelihood parameter estimate.

#### Author(s)

Kidus Asfaw

#### References

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, doi:10.1007/s11222020099573

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

#### See Also

```
likelihood evaluation algorithms: girf(), enkf(), bpfilter(), abf(), abfir()
Other likelihood maximization algorithms: ibpf(), ienkf(), iubf()
```

## **Examples**

```
# Complete examples are provided in the package tests
## Not run:
igirf(bm(U=2,N=4),Ngirf=2,
   rw.sd = rw_sd(rho=0.02,X1_0=ivp(0.02)),
   cooling.type="geometric",cooling.fraction.50=0.5,
   Np=10,Ninter=2,lookahead=1,Nguide=5)
## End(Not run)
```

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iubf

Iterated Unadapted Bagged Filter (IUBF)

#### **Description**

An algorithm for estimating the parameters of a spatiotemporal partially-observed Markov process. Running iubf causes the algorithm to perform a specified number of iterations of unadapted simulations with parameter perturbation and parameter resamplings. At each iteration, unadapted simulations are performed on a perturbed version of the model, in which the parameters to be estimated are subjected to random perturbations at each observation. After cycling through the data, each replicate's weight is calculated and is used to rank the bootstrap replicates. The highest ranking replicates are recycled into the next iteration. This extra variability introduced through parameter perturbation effectively smooths the likelihood surface and combats particle depletion by introducing diversity into particle population. As the iterations progress, the magnitude of the perturbations is diminished according to a user-specified cooling schedule.

## Usage

```
## S4 method for signature 'spatPomp'
iubf(
  object,
  Nubf = 1,
  Nrep_per_param,
  Nparam,
  nbhd,
  prop,
  rw.sd,
  cooling.type = c("geometric", "hyperbolic"),
  cooling.fraction.50,
  tol = (1e-18)^17,
  verbose = getOption("verbose"),
  ...
)
```

## Arguments

nbhd

object A spatPomp object.

Nubf The number of iterations to perform

Nrep\_per\_param The number of replicates used to estimate the likelihood at a parameter Nparam The number of parameters that will undergo the iterated perturbation

A neighborhood function with three arguments: object, time and unit. The function should return a list of two-element vectors that represent space-time neighbors of (u, n), which is represented by c(unit, time). See example below

for more details.

prop A numeric between 0 and 1. The top prop\*100% of the parameters are resam-

pled at each observation

iubf 39

rw.sd

specification of the magnitude of the random-walk perturbations that will be applied to some or all model parameters. Parameters that are to be estimated should have positive perturbations specified here. The specification is given using the rw\_sd function, which creates a list of unevaluated expressions. The latter are evaluated in a context where the model time variable is defined (as time). The expression ivp(s) can be used in this context as shorthand for

ifelse(time==time[1],s,0).

Likewise, ivp(s, lag) is equivalent to

ifelse(time==time[lag],s,0).

See below for some examples.

The perturbations that are applied are normally distributed with the specified s.d. If parameter transformations have been supplied, then the perturbations are applied on the transformed (estimation) scale.

cooling.type, cooling.fraction.50

specifications for the cooling schedule, i.e., the manner and rate with which the intensity of the parameter perturbations is reduced with successive filtering iterations. cooling.type specifies the nature of the cooling schedule. See below

(under "Specifying the perturbations") for more detail.

tol If the resampling weight for a particle is zero due to floating-point precision

issues, it is set to the value of tol since resampling has to be done.

verbose logical; if TRUE, diagnostic messages will be printed to the console.

... additional arguments are passed to pomp.

# Value

Upon successful completion, iubf() returns an object of class 'iubfd\_spatPomp'. This object contains the convergence record of the iterative algorithm with respect to the likelihood and the parameters of the model (which can be accessed using the traces attribute) as well as a final parameter estimate, which can be accessed using the coef(). The algorithmic parameters used to run iubf() are also included.

## Methods

The following methods are available for such an object:

coef extracts the point estimate

#### Author(s)

Kidus Asfaw

#### References

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

40 logLik

## See Also

```
likelihood evaluation algorithms: girf(), enkf(), bpfilter(), abf(), abfir()
Other likelihood maximization algorithms: ibpf(), ienkf(), igirf()
```

logLik

Log likelihood

# **Description**

Extract the estimated log likelihood.

## Usage

```
## S4 method for signature 'girfd_spatPomp'
logLik(object)

## S4 method for signature 'bpfilterd_spatPomp'
logLik(object)

## S4 method for signature 'abfd_spatPomp'
logLik(object)

## S4 method for signature 'iubfd_spatPomp'
logLik(object)

## S4 method for signature 'abfird_spatPomp'
logLik(object)

## S4 method for signature 'igirfd_spatPomp'
logLik(object)
```

# **Arguments**

object

fitted model object

# Value

a numeric which is the estimated log likelihood

lorenz 41

lorenz

Lorenz '96 spatPomp simulator

## **Description**

Generate a spatPomp object representing a U-dimensional stochastic Lorenz '96 process with N measurements made at times  $t_n = n*delta_obs$ , simulated using an Euler method with time increment delta\_t.

# Usage

```
lorenz(
    U = 5,
    N = 100,
    delta_t = 0.01,
    delta_obs = 0.5,
    regular_params = c(F = 8, sigma = 1, tau = 1)
)
```

# **Arguments**

U A length-one numeric signifying the number of spatial units for the process.

N A length-one numeric signifying the number of observations.

delta\_t A length-one numeric giving the Euler time step for the numerical solution.

delta\_obs A length-one numeric giving the time between observations.

regular\_params A named numeric vector containing the values of the F, sigma and tau parame-

ters. F=8 is a common value that causes chaotic behavior.

#### Value

An object of class 'spatPomp' representing a simulation from a U-dimensional Lorenz 96 model

## Author(s)

Edward L. Ionides

#### References

Lorenz, E. N. (1996) Predictability: A problem partly solved. *Proceedings of the seminar on predictability* 

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

## See Also

```
Other spatPomp model generators: bm(), bm2(), gbm(), he10(), measles()
```

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## **Examples**

```
# Complete examples are provided in the package tests
## Not run:
1 <- lorenz(U=5, N=100, delta_t=0.01, delta_obs=1)
# See all the model specifications of the object
spy(1)
## End(Not run)</pre>
```

measles

Measles in UK spatPomp generator

# Description

Generate a spatPomp object for measles in the top-U most populous cities in England and Wales. The model is adapted from He et al. (2010) with gravity transport following Park and Ionides (2020). The data are from Dalziel et al (2016).

# Usage

```
measles(
    U = 6,
    dt = 2/365,
    fixed_ivps = TRUE,
    S_0 = 0.032,
    E_0 = 5e-05,
    I_0 = 4e-05
)
```

# **Arguments**

U	A length-one numeric signifying the number of cities to be represented in the spatPomp object.
dt	a numeric (in unit of years) that is used as the Euler time-increment for simulating measles data.
fixed_ivps	a logical. If TRUE initial value parameters will be declared in the globals slot, shared for each unit, and will not be part of the parameter vector.
S_0	a numeric. If fixed_ivps=TRUE this is the initial proportion of all of the spatial units that are susceptible.
E_0	a numeric. If fixed_ivps=TRUE this is the initial proportion of all of the spatial units that are exposed.
I_0	a numeric. If fixed_ivps=TRUE this is the initial proportion of all of the spatial units that are infected.

# Value

An object of class 'spatPomp' representing a U-dimensional spatially coupled measles POMP model.

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#### Relationship to published analysis

This model was used to generate the results of Ionides et al (2021). However, their equation (6) is not exactly correct for the Binomial Gamma infinitesimal model used in the code, as shown by Proposition 5 of Breto and Ionides, 2011. If Poisson Gamma infinitesimal increments were used (Proposition 4 of Breto and Ionides, 2011) then (6) would be correct, but the resulting unbounded increments could break the non-negativity requirement for compartment membership. The same issue arises with the description in Park and Ionides (2020), though that analysis was based on a different model implementation since the spatPomp package was not yet available.

A difference between (6) of Ionides et al (2021) and (2.1) of He et al (2010) is that in (6) the mixing exponent  $\alpha$  is applied to  $(I_u/P_u)$  rather than just to  $I_u$ . In the context of He et al (2010) this changes the parameterization but has negligible effect on the model itself since  $P_u(t)$  is approximately constant and so changing its power can be compensated by a corresponding change in the transmission rate,  $\beta$ . In practice, models fitted to data have alpha close to 1, so this issue may be moot and this modeling mechanism may not be an effective empirical way to carry out the goal of making allowance for heterogeneous mixing.

The code here includes a cohort effect, c, following He et al (2010), that was not included by Ionides et al (2021). This effect leads to a non-differentiability of expected increments which is problematic for the spatPomp implementation of GIRF. For the results of Ionides et al (2021), this was set to c = 0.

The analysis of He et al (2010), and the model generated by he10(), use weekly aggregated cases. Weekly reports were not available beyond the 20 cites studied by He et al (2010) so measles() relies on the biweekly reports used by Ionides et al (2021) and Ionides & Park (2020).

It turns out to be an important detail of the model by He et al (2010) that a delay is included between birth and entry into the susceptible compartment. He et al (2010) found a 4 year delay fits the data. This value is fixed to be the variable birth\_delay in the code for measles(). The code for Ionides et al (2021) uses a 3 year delay, and the delay is not explained in the abbreviated model description. In measles() we have reverted to the 4 year delay identified by He et al (2010).

#### Note

This function goes through a typical workflow of constructing a typical spatPomp object (1-4 below). This allows the user to have a file that replicates the exercise of model building as well as function that creates a typical nonlinear model in epidemiology in case they want to test a new inference methodology. We purposely do not modularize this function because it is not an operational piece of the package and is instead useful as an example.

- 1. Getting a measurements data.frame with columns for times, spatial units and measurements.
- 2. Getting a covariates data.frame with columns for times, spatial units and covariate data.
- 3. Constructing model components (latent state initializer, latent state transition simulator and measurement model). Depending on the methods used, the user may have to supply a vectorfield to be integrated that represents the deterministic skeleton of the latent process.
- 4. Bringing all the data and model components together to form a spatPomp object via a call to spatPomp().

#### Author(s)

Edward L. Ionides

44 measles2

#### References

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

Dalziel, Benjamin D. et al. (2016) Persistent chaos of measles epidemics in the prevaccination United States caused by a small change in seasonal transmission patterns. *PLoS Computational Biology*, **12(2)**, e1004655. doi:10.5061/dryad.r4q34

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, doi:10.1007/s11222020099573

Breto, C. and Ionides, E.L. (2011) Compound Markov counting processes and their applications to modeling infinitesimally over-dispersed systems. Stochastic Processes and their Applications **121**, 2571-2591. doi:10.1016/j.spa.2011.07.005

#### See Also

```
measles_UK, city_data_UK
Other spatPomp model generators: bm(), bm2(), gbm(), he10(), lorenz()
```

## **Examples**

```
# Complete examples are provided in the package tests
## Not run:
m <- measles(U = 5)
# See all the model specifications of the object
spy(m)
## End(Not run)</pre>
```

measles2

Measles in UK: spatPomp generator with shared or unit-specific parameters

## **Description**

Generate a spatPomp object for measles in the top-U most populous cities in England and Wales. The model is adapted from He et al. (2010) with gravity transport following Park and Ionides (2019). The structure of this spatPomp is designed to accommodate shared and unit-specific parameters. If carrying out spatiotemporal iterated filtering for shared parameters via ibpf, it is necessary to have a unit-specific expansion and so these parameters should be included in expandedParNames. This model and data correspond to the biweekly analysis of Park and Ionides (2020) and Ionides et al (2021). There are small differences with the weekly model and data of He et al (2010) and Ionides, Ning and Wheeler (2022).

measles2 45

## Usage

```
measles2(
    U = 6,
    dt = 2/365,
    N = 391,
    expandedParNames = c("R0", "c", "A", "muIR", "muEI", "sigmaSE", "rho", "psi", "g",
        "S_0", "E_0", "I_0"),
    contractedParNames = NULL,
    simulated = FALSE,
    basic_params = c(alpha = 0.98, iota = 0.1, R0 = 30, c = 0.3, A = 0.5, muIR = 52, muEI =
    52, muD = 0.02, sigmaSE = 0.15, rho = 0.5, psi = 0.15, g = 400, S_0 = 0.032, E_0 =
    5e-05, I_0 = 4e-05)
)
```

#### **Arguments**

U An integer from 1 to 40 specifying the number of cities to be represented in the

spatPomp object.

dt a numeric (in unit of years) that is used as the Euler time-increment for simulat-

ing measles data

An integer from 1 to 391 specifying the number of time points.

expandedParNames

specifies parameters that are defined for each unit. This also allows unit perturbations for a parameter with a value shared across units.

contractedParNames

specifies parameters having a shared value across units. Remaining parameters that are neither expanded nor contracted are considered fixed, and will not have

a transformation defined for them.

simulated determines whether to return a simulation from the model or the UK measles

data

basic\_params A named vector used to specify shared parameters or unit-specific parameters

having common values for each unit.

#### Value

An object of class 'spatPomp' representing a U-dimensional spatially coupled measles POMP model.

## References

He, D., Ionides, E. L., and King, A. A. (2010). Plug-and-play inference for disease dynamics: measles in large and small populations as a case study. *Journal of the Royal Society Interface*, 7(43), 271-283. doi:10.1098/rsif.2009.0151

Park, J. and Ionides, E. L. (2020) Inference on high-dimensional implicit dynamic models using a guided intermediate resampling filter. *Statistics and Computing*, doi:10.1007/s11222020099573

Ionides, E. L., Asfaw, K., Park, J., and King, A. A. (2021). Bagged filters for partially observed interacting systems. *Journal of the American Statistical Association*, doi:10.1080/01621459.2021.1974867

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Ionides, E. L., Ning, N., and Wheeler, J. (2022). An iterated block particle filter for inference on coupled dynamic systems with shared and unit-specific parameters. *Statistica Sinica*, to appear. doi:10.48550/arXiv.2206.03837

## **Examples**

```
# Complete examples are provided in the package tests
## Not run:
m <- measles2(U = 5)
# See all the model specifications of the object
spy(m)
## End(Not run)</pre>
```

measlesUK

Measles in the United Kingdom

# **Description**

Measles case data from various cities and towns in England and Wales during the pre-vaccine era.

# **Details**

Data includes bi-weekly case counts as well as births and population from 40 cities and towns.

#### Value

a 'data.frame' of the 40 largest cities and towns in the UK and Wales, their latitude, longitude and bi-weekly measles case counts, population and birthrates.

## References

Dalziel, Benjamin D. et al. (2016) Persistent chaos of measles epidemics in the prevaccination United States caused by a small change in seasonal transmission patterns. *PLoS Computational Biology*, **12(2)**, e1004655. doi:10.5061/dryad.r4q34

#### See Also

Other datasets: city\_data\_UK

munit\_measure 47

# Description

munit\_measure returns a moment-matched parameter set given an empirically calculated measurement variance and latent states. This is used in girf() and igirf() when they are run with kind='moment'.

# Usage

```
## S4 method for signature 'spatPomp'
munit_measure(object, x, vc, unit, time, params, Np = 1)
```

# **Arguments**

object	An object of class spatPomp
x	A state vector for all units
vc	The empirically calculated variance used to perform moment-matching
unit	The unit for which to obtain a moment-matched parameter set
time	The time for which to obtain a moment-matched parameter set
params	parameters to use to obtain a moment-matched parameter set
Np	Number of particle replicates for which to get parameter sets

## Value

An array with dimensions  $\dim(\operatorname{array.params})[1]$  by  $\dim(x)[2]$  by  $\operatorname{length}(\operatorname{unit})$  by  $\operatorname{length}(\operatorname{time})$  representing the moment-matched parameter  $\operatorname{set}(s)$  corresponding to the variance of the measurements, vc, and the states, x.

## Author(s)

Kidus Asfaw

# **Examples**

```
# Complete examples are provided in the package tests ## Not run: b <- bm(U=3) s <- states(b)[,1,drop=FALSE] rownames(s) -> rn dim(s) <- c(3,1,1) dimnames(s) <- list(variable=rn, rep=NULL) p <- coef(b); names(p) -> rnp <math>dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp) o <- obs(b)[,1,drop=FALSE] array.params <- array(p,
```

48 plot

plot

Plotting spatPomp data

# **Description**

Visualize spatPomp data

Diagnostic plot for igirf()

Visualize spatPomp data

# Usage

```
## S4 method for signature 'igirfd_spatPomp'
plot(x, params = names(coef(x)), ncol = 3)

## S4 method for signature 'spatPomp'
plot(x, type = c("1", "h"), log = F, plot_unit_names = T, ...)
```

# **Arguments**

x	a spatPomp object	
params	the names of the parameters for which the user would like to see a trace plot	
ncol	the number of columns in the grid plot	
type	for visualizing an object of class spatPomp, the user can obtain a grid of line plots by default ('1') or a heat map by supplying argument 'h'.	
log	should the data be log-transformed before plotting? This helps in contexts where there are spikes that could take away attention from the dynamics illustrated by the rest of the data.	
plot_unit_names		
	allows suppression of unit names when making a heat map for a large number of units	

for visualizing an object of class spatPomp, the user can add arguments like nrow to specify the number of rows in the grid.

print 49

## Value

a ggplot facet plot of class 'gg' and 'ggplot' visualizing the convergence record of running igirf() with respect to the likelihood and the parameters of the model.

a ggplot plot of class 'gg' and 'ggplot' visualizing the time series data over multiple spatial units via a tile-plot.

print

Print methods

# Description

Prints its argument.

## Usage

```
## S4 method for signature 'spatPomp'
print(x)
```

## **Arguments**

Х

a spatPomp object

#### Value

An object of class 'spatPomp' is returned \*invisibly\*. The user is notified on the console only the class of the object.

#### Note

Use spy() to see model components of x instead.

runit\_measure

runit\_measure

# **Description**

runit\_measure simulates a unit's observation given the entire state

## Usage

```
## S4 method for signature 'spatPomp'
runit_measure(object, x, unit, time, params, log = FALSE)
```

simulate

# **Arguments**

object	An object of class spatPomp
х	A state vector for all units
unit	The unit for which to simulate an observation
time	The time for which to simulate an observation
params	parameters to use to simulate an observation
log	logical; should the density be returned on log scale?

# Value

A matrix with the simulated observation corresponding to state x and unit unit with parameter set params.

# Author(s)

Kidus Asfaw

# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
runit_measure(b, x=s, unit=2, time=1, params=p)
## End(Not run)</pre>
```

simulate

Simulation of a spatiotemporal partially-observed Markov process

# Description

simulate generates simulations of the latent and measurement processes.

simulate 51

## Usage

```
## S4 method for signature 'spatPomp'
simulate(
  object,
  nsim = 1,
  seed = NULL,
  format = c("spatPomps", "data.frame"),
  include.data = FALSE,
  ...
)
```

# **Arguments**

object optional; if present, it should be a data frame or a 'pomp' object.

nsim number of simulations.

seed optional integer; if set, the pseudorandom number generator (RNG) will be ini-

tialized with seed. The RNG will be restored to its original state afterward.

format the format of the simulated results. If the argument is set to 'spatPomps', the

default behavior, then the output is a list of spatPomp objects. Options are

'spatPomps' and 'data.frame'.

include.data if TRUE, the original data and covariates (if any) are included (with .id = "data").

This option is ignored unless format = "data.frame".

. . . additional arguments are passed to pomp.

#### Value

if format='spatPomps' and nsim=1 an object of class 'spatPomp' representing a simulation from the model in object is returned. If format='spatPomps' and nsim>1 a list of class 'spatPomp' objects is returned. If format='data.frame' then a class 'data.frame' object is returned.

# Author(s)

Kidus Asfaw

# References

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

## **Examples**

```
# Complete examples are provided in the package tests
## Not run:
# Get a spatPomp object
b <- bm(U=2, N=5)
# Get 2 simulations from same model as data.frame
sims <- simulate(b, nsim=2, format='data.frame')</pre>
```

```
## End(Not run)
```

spatPomp

Constructor of the spatPomp object

## **Description**

This function constructs a class 'spatPomp' object, encoding a spatiotemporal partially observed Markov process (SPATPOMP) model together with a uni- or multi-variate time series on a collection of units. Users will typically develop a POMP model for a single unit before embarking on a coupled SpatPOMP analysis. Consequently, we assume some familiarity with **pomp** and its description by King, Nguyen and Ionides (2016). The spatPomp class inherits from pomp with the additional unit structure being a defining feature of the resulting models and inference algorithms.

## Usage

```
spatPomp(
  data,
  units,
  times,
  covar,
  t0,
  eunit_measure,
 munit_measure,
  vunit_measure,
  dunit_measure,
  runit_measure,
  rprocess,
  rmeasure,
  dprocess,
  dmeasure,
  skeleton,
  rinit,
  rprior,
  dprior,
  unit_statenames,
  unit_accumvars,
  shared_covarnames,
  globals,
  paramnames,
  params,
  cdir,
  cfile,
  shlib.args,
 PACKAGE,
```

```
partrans,
compile = TRUE,
verbose = getOption("verbose", FALSE)
)
```

#### **Arguments**

data

either a dataframe holding the spatiotemporal data, or an object of class 'spat-Pomp', i.e., the output of another **spatPomp** calculation. If dataframe, the user must provide the name of the times column using the times argument and the spatial unit column name using the units argument. The dataframe provided should be sorted in increasing order of time and unit name respectively, i.e. observation 1 in unit A should come before observation 1 in unit B, which should come before observation 2 in unit A.

units

when data is a data. frame this is the name of the column containing the spatial

times

the sequence of observation times. times must indicate the column of observation times by name or index. The time vector must be numeric and non-decreasing.

covar

An optional dataframe for supplying covariate information. If provided, there must be two columns that provide the observation time and the observation spatial unit with the same names and arrangement as the data.

t0

The zero-time, i.e., the time of the initial state. This must be no later than the time of the first observation, i.e.,  $t0 \le times[1]$ .

. . .

If there are arguments that the user would like to pass to **pomp**'s basic constructor function's ... argument, this argument passes them along. Not recommended for this version of **spatPomp**.

eunit\_measure

Evaluator of the expected measurement given the latent states and model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only C snippets are accepted. The C snippet should assign the scalar approximation to the expected measurement to the pre-defined variable ey given the latent state and the parameters. For more information, see the examples section below.

munit\_measure

Evaluator of a moment-matched parameter set (like the standard deviation parameter of a normal distribution or the size parameter of a negative binomial distribution) given an empirical variance estimate, the latent states and all model parameters. Only Csnippets are accepted. The Csnippet should assign the scalar approximation to the measurement variance parameter to the pre-defined variable corresponding to that parameter, which has been predefined with a M\_ pre-fix. For instance, if the moment-matched parameter is psi, then the user should assign M\_psi to the moment-matched value. For more information, see the examples section below.

vunit\_measure

Evaluator of the theoretical measurement variance given the latent states and model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only C snippets are accepted. The C snippet should assign the scalar approximation to the

measurement variance to the pre-defined variable vc given the latent state and the parameters. For more information, see the examples section below.

dunit\_measure

Evaluator of the unit measurement model density given the measurement, the latent states and model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only Csnippets are accepted. The Csnippet should assign the scalar measurement density to the pre-defined variable lik. The user is encouraged to provide a logged density in an if condition that checks whether the predefined give\_log variable is true. For more information, see the examples section below.

runit\_measure

Simulator of the unit measurement model given the latent states and the model parameters. The unit variable is pre-defined, which allows the user to specify differing specifications for each unit using if conditions. Only Csnippets are accepted. The Csnippet should assign the scalar measurement density to the pre-defined which corresponds to the name of the observation for each unit (e.g. cases for the measles spatPomp example). For more information, see the examples section below.

rprocess

simulator of the latent state process, specified using one of the rprocess plugins. Setting rprocess=NULL removes the latent-state simulator. For more information, see rprocess specification for the documentation on these plugins.

rmeasure

simulator of the measurement model, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rmeasure=NULL removes the measurement model simulator. For more information, see rmeasure specification.

dprocess

evaluator of the probability density of transitions of the unobserved state process. Setting dprocess=NULL removes the latent-state density evaluator. For more information, see dprocess specification.

dmeasure

evaluator of the measurement model density, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting dmeasure=NULL removes the measurement density evaluator. For more information, see dmeasure specification.

skeleton

optional; the deterministic skeleton of the unobserved state process. Depending on whether the model operates in continuous or discrete time, this is either a vectorfield or a map. Accordingly, this is supplied using either the vectorfield or map factions. For more information, see skeleton specification. Setting skeleton=NULL removes the deterministic skeleton.

rinit

simulator of the initial-state distribution. This can be furnished either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. Setting rinit=NULL sets the initial-state simulator to its default. For more information, see rinit specification.

rprior

optional; prior distribution sampler, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see prior specification. Setting rprior=NULL removes the prior distribution sampler.

dprior

optional; prior distribution density evaluator, specified either as a C snippet, an R function, or the name of a pre-compiled native routine available in a dynamically loaded library. For more information, see prior specification. Setting

dprior=NULL resets the prior distribution to its default, which is a flat improper prior.

unit\_statenames

The names of the components of the latent state. E.g. if the user is constructing an joint SIR model over many spatial units, c('S','I','R') would be passed.

unit\_accumvars a subset of the unit\_statenames argument that are accumulator variables. See accumvars for more on the concept of **pomp** accumulator variables.

shared\_covarnames

If covar is supplied, covariates that are shared must still be specified for each unit, i.e., rows with equal values for the same time over all units must be supplied. However, if such covariates exists, supply the names using this argument.

optional character or C snippet; arbitrary C code that will be hard-coded into the shared-object library created when C snippets are provided. If no C snippets are used, globals has no effect.

optional character vector; names of model parameters. It is typically only necessary to supply paramnames when C snippets are in use.

optional; named numeric vector of parameters. This will be coerced internally to storage mode double.

optional character variable. cdir specifies the name of the directory within which C snippet code will be compiled. By default, this is in a temporary directory specific to the R session. One can also set this directory using the pomp\_cdir global option.

optional character variable. cfile gives the name of the file (in directory cdir) into which C snippet codes will be written. By default, a random filename is used. If the chosen filename would result in over-writing an existing file, an error is generated.

optional character variables. Command-line arguments to the R CMD SHLIB call that compiles the C snippets. One can, for example, specify libraries against which the C snippets are to be linked. In doing so, take care to make sure the appropriate header files are available to the C snippets, e.g., using the globals argument. See Csnippet for more information.

optional character; the name (without extension) of the external, dynamically loaded library in which any native routines are to be found. This is only useful if one or more of the model components has been specified using a precompiled dynamically loaded library; it is not used for any component specified using C snippets. PACKAGE can name at most one library.

Many algorithms for parameter estimation search an unconstrained space of parameters. When working with such an algorithm and a model for which the parameters are constrained, it can be useful to transform parameters. One should supply the partrans argument via a call to parameter\_trans. For more information, see parameter\_trans. Setting partrans=NULL removes the parameter

optional parameter transformations, constructed using parameter\_trans.

transformations, i.e., sets them to the identity transformation.

logical; if FALSE, compilation of the C snippets will be postponed until they are needed.

logical; if TRUE, diagnostic messages will be printed to the console.

globals

paramnames

params

cdir

cfile

shlib.args

**PACKAGE** 

partrans

compile

verbose

#### **Details**

One implements a SPATPOMP model by specifying some or all of its basic components, including:

rinit, the simulator from the distribution of the latent state process at the zero-time;

**rprocess**, the transition simulator of the latent state process;

**dunit\_measure**, the evaluator of the conditional density at a unit's measurement given the unit's latent state;

**eunit\_measure,** the evaluator of the expectation of a unit's measurement given the unit's latent state:

**munit\_measure,** the evaluator of the moment-matched parameter set given a unit's latent state and some empirical measurement variance;

vunit\_measure, the evaluator of the variance of a unit's measurement given the unit's latent state;

runit\_measure, the simulator of a unit's measurement conditional on the unit's latent state;

**dprocess**, the evaluator of the density for transitions of the latent state process;

**rmeasure**, the simulator of the measurements conditional on the latent state;

**dmeasure**, the evaluator of the conditional density of the measurements given the latent state;

rprior, the simulator from a prior distribution on the parameters;

dprior, the evaluator of the prior density;

skeleton, which computes the deterministic skeleton of the unobserved state process;

partrans, which performs parameter transformations.

The basic structure and its rationale are described in Asfaw et al. (2020).

Each basic component is supplied via an argument of the same name to spatPomp(). The five unit-level model components must be provided via C snippets. The remaining components, whose behaviors are inherited from **pomp** may be furnished using C snippets, R functions, or pre-compiled native routine available in user-provided dynamically loaded libraries.

#### Value

An object of class 'spatPomp' representing observations and model components from the spatiotemporal POMP model.

#### Author(s)

Kidus Asfaw, Edward L. Ionides, Aaron A. King

#### References

Asfaw, K., Park, J., Ho, A., King, A. A., and Ionides, E. L. (2020) Partially observed Markov processes with spatial structure via the R package spatPomp. *ArXiv*: 2101.01157. doi:10.48550/arXiv.2101.01157

King, A. A., Nguyen, D. and Ionides, E. L. (2016) Statistical Inference for Partially Observed Markov Processes via the R Package pomp. *Journal of Statistical Software*, **69**(**12**), 1–43. doi:10.18637/jss.v069.i12

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spatPomp-class

An S4 class to represent a spatiotemporal POMP model and data.

## Description

An S4 class to represent a spatiotemporal POMP model and data.

## **Slots**

unit\_names A vector containing the spatial units of a spatiotemporal POMP.

unit\_statenames A vector containing the state names such that appending the unit indices to the unit statenames will result in the each unit's corresponding states.

unit\_obsnames A vector of observation types for a spatial unit.

eunit\_measure A pomp\_fun representing the expected measurement for each spatial unit given its states.

dunit\_measure A pomp\_fun representing the unit measurement density for each spatial unit.

runit\_measure A pomp\_fun representing the unit observation simulator.

spatPomp\_Csnippet

C snippets

## Description

spatPomp\_Csnippet() is used to provide snippets of C code that specify model components. It functions similarly to Csnippet() from the **pomp** package; in fact, the output of spatPomp\_Csnippet is an object of class Csnippet. It additionally provides some arguments that allow the user to stay focused on model development in the spatiotemporal context where model size grows.

## Usage

```
## S4 method for signature 'character'
spatPomp_Csnippet(
  code,
  method = "",
  unit_statenames,
  unit_obsnames,
  unit_covarnames,
  unit_ivpnames,
  unit_jparamnames,
  unit_vfnames
)
```

## Arguments

code encodes a component of a spatiotemporal POMP model using C code

method a character string matching the name of the 'spatPomp' argument which the

code is designed to specify. This argument is ignored unless needed to correctly

specify the Csnippet.

unit\_statenames

a subset of the unit\_statenames slot of the spatPomp object for which we are writing a model. This argument allows the user to get variables that can be indexed conveniently to update states and measurements in a loop. See examples

for more details.

unit\_obsnames a subset of the unit\_obsnames slot of the spatPomp object for which we are

writing a model. This argument allows the user to get variables that can be indexed conveniently to update states and measurements in a loop. See examples

for more details.

unit\_covarnames

if the model has covariate information for each unit, the names of the covariates for each unit can be supplied to this argument. This allows the user to get variables that can be indexed conveniently to use incorporate the covariate

information in a loop. See examples for more details.

unit\_ivpnames

This argument is particularly useful when specifying the rinit model component. The paramnames argument to the spatPomp() constructor often has names for initial value parameters for the latent states (e.g. S1\_0, S2\_0 for the the quantity of susceptibles at unit 1 and unit 2 at the initial time in an SIR model). By supplying unit\_ivpnames, we can get variables that can be easily indexed to reference the initial value parameters (in the previous example, unit\_ivpnames=c('S') we can get a variable named S\_0 that we can index as S\_0[0] and S\_0[1] to refer to S1\_0 and S2\_0). See examples for more details.

unit\_paramnames

This argument is particularly useful when there are non-initial value parameters

that are unit-specific.

unit\_vfnames

This argument is particularly useful when specifying the skeleton model component. For all components of the latent state, the user can assume a variable defining the time-derivative is pre-defined (e.g. DS1 and DS2 for the time-derivative of the quantity of the susceptibles at unit 1 and unit 2 in an SIR model). By supplying unit\_vfnames, we can get variables that can be easily indexed to reference these variables (in the previous example, setting unit\_vfnames=c('S')

gets us a variable named DS that we can index as DS[0] and DS[1] to refer to

DS1 and DS2). See examples for more details.

#### Value

An object of class 'Csnippet' which represents a model specification in C code.

# Author(s)

Kidus Asfaw

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## **Examples**

```
# Set initial states for Brownian motion
bm_rinit <- spatPomp_Csnippet(</pre>
  method = "rinit",
  unit_statenames = c("X"),
  unit_ivpnames = c("X"),
  code = "
    for (int u = 0; u < U; u++) {
      X[u]=X_0[u];
    }
)
# Skeleton for Brownian motion
bm_skel <- spatPomp_Csnippet(</pre>
  method = "skeleton",
  unit_statenames = c("X"),
  unit_vfnames = c("X"),
  code = "
      for (int u = 0; u < U; u++) {
        DX[u] = 0;
)
```

unit\_names

Unit names of a spatiotemporal model

# Description

unit\_names outputs the contents of the unit\_names slot of a spatPomp object. The order in which the units appear in the output vector determines the order in which latent states and observations for the spatial units are stored.

# Usage

```
## S4 method for signature 'spatPomp'
unit_names(x)
```

# Arguments

Х

a spatPomp object

## Value

A character vector with the unit names used to create the 'spatPomp' object.

vec\_rmeasure

vec_dmeasure	Vector of measurement densities	

# **Description**

Evaluate the unit measurement model density function for each unit. This method is used primarily as part of likelihood evaluation and parameter inference algorithms.

## Usage

```
## S4 method for signature 'spatPomp'
vec_dmeasure(object, y, x, units, times, params, log = FALSE, ...)
```

## **Arguments**

object	a spatPomp object
У	numeric; measurements whose densities given the latent states are evaluated
X	numeric; state at which conditional measurement densities are evaluated
units	numeric; units at which measurement densities are evaluated
times	numeric; time at which measurement densities are evaluated
params	numeric; parameter set at which measurement densities is evaluated
log	logical; should the outputted measurement densities be on log scale?
	additional parameters will be ignored

# Value

An array of dimension length(unit\_names(object)) by dim(x)[2] by dim(x)[3] representing each unit's measurement density assessed for each replicate in x for each observation time.

# Author(s)

Kidus Asfaw

vec_rmeasure Vector of simulated measurements
---

# Description

Simulate from the unit measurement model density function for each unit

#### Usage

```
## S4 method for signature 'spatPomp'
vec_rmeasure(object, x, times, params, ...)
```

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# **Arguments**

object	a spatPomp	object
--------	------------	--------

x numeric; state at which measurements are simulated times numeric; time at which measurements are simulated

params numeric; parameter set at which measurements are simulated

... additional parameters will be ignored

## Value

An array of dimension length(unit\_names(object)) by dim(x)[2] by dim(x)[3] representing each unit's simulated measurement assessed for each replicate in x for each observation time.

## Author(s)

Kidus Asfaw

# **Description**

vunit\_measure evaluates the variance of a unit's observation given the entire state

# Usage

```
## S4 method for signature 'spatPomp'
vunit_measure(object, x, unit, time, params, Np = 1)
```

# **Arguments**

object	An object of class spatPomp
X	A state vector for all units

unit The unit for which to evaluate the variance
time The time for which to evaluate the variance
params parameters at which to evaluate the unit variance

Np numeric; defaults to 1 and the user need not change this

#### Value

A matrix with the unit measurement variance implied by the state, x, and the parameter set params for unit unit.

# Author(s)

Kidus Asfaw

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# **Examples**

```
# Complete examples are provided in the package tests
## Not run:
b <- bm(U=3)
s <- states(b)[,1,drop=FALSE]
rownames(s) -> rn
dim(s) <- c(3,1,1)
dimnames(s) <- list(variable=rn, rep=NULL)
p <- coef(b); names(p) -> rnp
dim(p) <- c(length(p),1); dimnames(p) <- list(param=rnp)
o <- obs(b)[,1,drop=FALSE]
vunit_measure(b, x=s, unit=2, time=1, params=p)
## End(Not run)</pre>
```

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