

$$\int_{U(r)} H dr = \int_{U(r)} H dr = \frac{I}{2\pi r_0} \int_{U(r)} dr = \frac{I}{2\pi r_0} \int_{U(r)} dr = I$$